

## LOW PASS BUTTRERWORTH USING BILINEAR

```
clear all;
wp=input('enter the the passband freq: ');
ws=input('enter the the stopband freq: ');
ap=input('enter the the passband gain: ');
as=input('enter the the stopband gain: ');
T=input('enter sampling interval: ');
Fs=1/T;
rp=-20*log10(ap);
disp('the passbad ripple of the filter ');rp
rs=-20*log10(as);
disp('the stopband ripple of the filter ');rs
omp=(2/T)*tan(wp/2);
disp('the analog passband freq of the filter '); omp
oms=(2/T)*tan(ws/2);
disp('the analog stopband freq of th filter ');oms
[N,wc]=buttord(omp,oms,rp,rs,'s');
disp('the order of th filter ');N
disp('the cutoff freq of th filter ');wc
[bn,an]=butter(N,1,'s');
disp('the normalized transfer function');
HSn=tf(bn,an)
[b,a]=butter(N,wc,'s');
disp('the analog transfer function');
HS=tf(b,a)
[num,den]=bilinear(b,a,1/T);
disp('the digital transfer function');
HZ=tf(num,den,T)
w=0:pi/16:pi;
disp('the frequency response is');
HW=freqz(num,den,w)
HW=freqz(num,den,w);
disp('the magnitue response is');
HW_mag=abs(HW)
plot(w/pi,HW_mag,'k');grid
title('magnitue resp of butterworth 2nd order lowpass filter');
xlabel('normalized freq');
ylabel('magnitue');
```

## ANSWER

the the passband gain: 0.6  
enter the the passband freq: 0.35\*pi  
enter the the stopband freq: 0.7\*pi  
enter enter the the stopband gain: 0.1  
enter sampling interval: 0.1  
the passbad ripple of the filter rp = 4.4370  
the stopband ripple of the filter rs = 20  
the analog passband freq of the filter omp = 12.2560  
the analog stopband freq of th filter oms = 39.2522

the order of th filter N = 2  
the cutoff freq of th filter  $\omega_c = 12.4439$

the normalized transfer function

Transfer function:

$$\frac{1}{s^2 + 1.414 s + 1}$$

the analog transfer function

Transfer function:

$$\frac{154.8}{s^2 + 17.6 s + 154.8}$$

the digital transfer function

Transfer function:

$$\frac{0.1708 z^2 + 0.3415 z + 0.1708}{z^2 - 0.5407 z + 0.2237}$$

Sampling time: 0.1

the frequency response is HW =

Columns 1 through 6

1.0000      0.9743 - 0.2237i   0.8885 - 0.4474i   0.7215 - 0.6526i   0.4654 - 0.7869i   0.1696 - 0.7865i

Columns 7 through 12

-0.0658 - 0.6518i   -0.1837 - 0.4632i   -0.2063 - 0.2962i   -0.1805 - 0.1763i   -0.1388 - 0.0987i   -0.0972 - 0.0514i

Columns 13 through 17

-0.0617 - 0.0241i   -0.0343 - 0.0095i   -0.0151 - 0.0027i   -0.0037 - 0.0003i   -0.0000 - 0.0000i

the magnitude response is HW\_mag =

Columns 1 through 12

1.0000   0.9997   0.9948   0.9729   0.9142   0.8046   0.6551   0.4983   0.3610   0.2523   0.1703  
0.1099

Columns 13 through 17

0.0663   0.0356   0.0153   0.0038   0.0000

## HIGH PASS BUTTRERWORTH USING BILINEAR

```
Clc;
Close all;
clear all;
wp=input('enter the the passband freq: ');
ws=input('enter the the stopband freq: ');
ap=input('enter the the passband gain: ');
as=input('enter the the stopband gain: ');
T=input('enter sampling interval: ');
Fs=1/T;
rp=-20*log10(ap);
disp('the passbad ripple of the filter ');rp
rs=-20*log10(as);
disp('the stopband ripple of the filter ');rs
omp=(2/T)*tan(wp/2);
disp('the analog passband freq of the filter '); omp
oms=(2/T)*tan(ws/2);
disp('the analog stopband freq of the filter ');oms
[N,wc]=buttord(omp,oms,rp,rs,'s');
disp('the order of th filter ');N
disp('the cutoff freq of th filter ');wc
[bn,an]=butter(N,1,'s');
disp('normalized transfer function is ');
HSn=tf(bn,an)
[b,a]=butter(N,wc,'high','s');
disp('the analog transfer function');
HS=tf(b,a)
[num,den]=bilinear(b,a,1/T);
disp('the digital transfer function');
HZ=tf(num,den,T)
w=0:pi/16:pi;
disp('the frequency response is');
HW=freqz(num,den,w)
disp('the magnitue response is');
HW_mag=abs(HW)
plot(w/pi,HW_mag,'k');grid
title('magnitue resp of butterworth 2nd order lowpass filter');
xlabel('normalized freq');
ylabel('magnitue');
```

### ANS

enter the the passband freq:  $0.35\pi$   
enter the the stopband freq:  $0.7\pi$   
enter the the passband gain: 0.6  
enter the the stopband gain: 0.1  
enter sampling interval: 0.1  
the passbad ripple of the filter  $rp = 4.4370$

the stopband ripple of the filter  $rs = 20$   
the analog passband freq of the filter  $omp = 12.2560$   
the analog stopband freq of the filter  $oms = 39.2522$   
the order of th filter  $N = 2$

the cutoff freq of th filter  $\omega_c = 12.4439$

normalized transfer function is

Transfer function:

$$\frac{1}{s^2 + 1.414 s + 1}$$

the analog transfer function

Transfer function:

$$\frac{s^2}{s^2 + 17.6 s + 154.8}$$

the digital transfer function

Transfer function:

$$\frac{0.4411 z^2 - 0.8822 z + 0.4411}{z^2 - 0.5407 z + 0.2237}$$

Sampling time: 0.1

the frequency response is HW =

Columns 1 through 6

0.0000 -0.0244 + 0.0056i -0.0908 + 0.0457i -0.1715 + 0.1551i -0.2063 + 0.3488i -  
0.1252 + 0.5805i

Columns 7 through 12

0.0759 + 0.7517i 0.3196 + 0.8059i 0.5330 + 0.7652i 0.6922 + 0.6762i 0.8032 + 0.5709i  
0.8786 + 0.4646i

Columns 13 through 17

0.9295 + 0.3629i 0.9632 + 0.2666i 0.9845 + 0.1750i 0.9962 + 0.0867i 1.0000 + 0.0000i

the magnitude response is HW\_mag =

Columns 1 through 12

0.0000 0.0251 0.1017 0.2313 0.4052 0.5938 0.7555 0.8670 0.9326 0.9676  
0.9854 0.9939

Columns 13 through 17

0.9978 0.9994 0.9999 1.0000 1.0000

## BANDPASS BUTTRERWORTH USING BILINEAR

```
clc;
close all;
clear all;
wp=input('enter the the passband freq in rad : ');
ws=input('enter the the stopband freq in rad : ');
rp=input('enter the the passband ripple: ');
rs=input('enter the the stopband ripple: ');
fs=input('enter sampling frequency : ');
T=1/fs;
omp=(2/T)*tan(wp/2);
disp('the analog passband freq of the filter '); omp
oms=(2/T)*tan(ws/2);
disp('the analog stopband freq of the filter '); oms
[N,wc]=buttord(omp,oms,rp,rs,'s');
disp('the order of th filter ');N
disp('the cuttoff freq of th filter ');wc
[bn,an]=butter(N,1,'s');
disp('normalized transfer function is ');
HSn=tf(bn,an)
[b,a]=butter(N,wc,'bandpass','s');
disp('the analog transfer function');
HS=tf(b,a)
[num,den]=bilinear(b,a,1/T);
disp('the digital transfer function');
HZ=tf(num,den,T)
w=0:pi/16:pi;
disp('the frequency response is');
HW=freqz(num,den,w)
disp('the magnitue response is');
HW_mag=abs(HW)
plot(w/pi,HW_mag,'k');grid
title('magnitude resp of butterworth 2nd order lowpass filter');
xlabel('normalized freq');
ylabel('magnitue');
```

## ANS

enter the the passband freq in rad : [0.4\*pi 0.6\*pi]

enter the the stopband freq in rad : [0.1\*pi 0.8\*pi]

enter the the passband ripple: 1

enter the the stopband ripple: 20

enter sampling frequency : 1000

the analog passband freq of the filter omp = 1.0e+003 \* 1.4531 2.7528

the analog stopband freq of the filter oms = 1.0e+003 \* 0.3168 6.1554

the order of the filter N = 3

the cuttoff freq of the filter wc = 1.0e+003 \* 1.0946 3.6543

normalized transfer function is

Transfer function:

$$\frac{1}{s^3 + 2s^2 + 2s + 1}$$

the analog transfer function

Transfer function:

$$\frac{1.677e010 s^3}{s^6 + 5119 s^5 + 2.51e007 s^4 + 5.773e010 s^3 + 1.004e014 s^2 + 8.191e016 s + 6.4e019}$$

the digital transfer function

Transfer function:

$$\frac{0.07797 z^6 - 2.46e-015 z^5 - 0.2339 z^4 - 1.725e-015 z^3 + 0.2339 z^2 + 1.98e-016 z - 0.07797}{z^6 - 4.025e-016 z^5 + 0.7958 z^4 - 3.189e-016 z^3 + 0.502 z^2 - 3.352e-016 z + 0.08245}$$

Sampling time: 0.001

the frequency response is HW =

Columns 1 through 6

-0.0000 -0.0005 - 0.0020i -0.0095 - 0.0160i -0.0604 - 0.0493i -0.2496 - 0.0444i -0.5142 + 0.4138i

Columns 7 through 12

0.1510 + 0.9533i 0.8060 + 0.5911i 1.0000 + 0.0000i 0.8060 - 0.5911i 0.1510 - 0.9533i -0.5142 - 0.4138i

Columns 13 through 17

-0.2496 + 0.0444i -0.0604 + 0.0493i -0.0095 + 0.0160i -0.0005 + 0.0020i 0.0000 + 0.0000i

the magnitude response is HW\_mag =

Columns 1 through 12

0.0000 0.0021 0.0186 0.0779 0.2535 0.6600 0.9651 0.9995 1.0000 0.9995 0.9651 0.6600

Columns 13 through 17

0.2535 0.0779 0.0186 0.0021 0.0000