

SQUARESTABLE

$1^2 = 1$	1	2	3	4	5	6	7	8	9	10
$2^2 = 4$	2	4	6	8	10	12	14	16	18	20
$3^2 = 9$	3	6	9	12	15	18	21	24	27	30
$4^2 = 16$	4	8	12	16	20	24	28	32	36	40
$5^2 = 25$	5	10	15	20	25	30	35	40	45	50
$6^2 = 36$	6	12	18	24	30	36	42	48	54	60
$7^2 = 49$	7	14	21	28	35	42	49	56	63	70
$8^2 = 64$	8	16	24	32	40	48	56	64	72	80
$9^2 = 81$	9	18	27	36	45	54	63	72	81	90
$10^2 = 100$	10	20	30	40	50	60	70	80	90	100
$11^2 = 121$	11	22	33	44	55	66	77	88	99	110
$12^2 = 144$	12	24	36	48	60	72	84	96	108	120
$13^2 = 169$	13	26	39	52	65	78	91	104	117	130
$14^2 = 196$	14	28	42	56	70	84	98	112	126	140
$15^2 = 225$	15	30	45	60	75	90	105	120	135	150
$16^2 = 256$	<u>16</u>	32	48	64	80	96	112	128	144	160
$17^2 = 289$	17	34	51	68	85	102	119	136	153	170
$18^2 = 324$	18	36	54	72	90	108	126	144	162	180
$19^2 = 361$	19	38	57	76	95	114	133	152	171	190
$20^2 = 400$	20	40	60	80	100	120	140	160	180	200
$21^2 = 441$	21	42	63	84	105	126	147	168	189	210
$22^2 = 484$	22	44	66	88	110	132	154	176	198	220
$23^2 = 529$	23	46	69	92	115	138	161	184	207	230
$24^2 = 576$	24	48	72	96	120	144	168	192	216	240
$25^2 = 625$	25	50	75	100	125	150	175	200	225	250

DIVISIBILITY:

- 2 - Any even numbers or numbers which end with 0.
- 3 - Sum of the digits if divisible by 3.
- 4 - Last two digits are 00 or divisible by 4.
- 5 - Last digit should be 5 or 0.
- 6 - If divisible by 2 and 3.
- 8 - Last three digits are 000 or divisible by 8.
- 9 - Sum of the digits if divisible by 9.
- 10 - Last digit of the number should be 0.
- 11 - Difference of alternate digits either a or divisible by 11.

$\sqrt{2} = 1.414$

$\sqrt{3} = 1.732$

FORMULAE : ARITHMATIC

1. 0 is an even number
2. 1 is neither prime nor compound.
3. i) Natural numbers $\rightarrow N - 1, 2, 3, \dots$ all the positive integers. [Not 0]
 ii) Integers $\rightarrow I$ - All positive and negative numbers including 0, $0, \pm 1, \pm 2, \dots$
 iii) Rational Numbers, $Q \rightarrow$ Numbers in the form m/n where $n \neq 0, -2, -\frac{2}{3}, 3, \dots$
 iv) Irrational Numbers, \rightarrow Which are not in the form $m/n, \sqrt{2}, \sqrt[3]{3}, 2 \pm \sqrt{3}, \sqrt{5}/2, \dots$
 v) Real Numbers, $R \rightarrow$ All rational and irrational numbers, $2, \sqrt{2}, 0.2, \dots$
4. Product of two numbers/fractions = their L.C.M \times H.C.F
5. Dividend = Divisor \times Quotient + Remainder
6. i) Proper fractions : Fractions less than 1, i.e. $\frac{1}{2}, \frac{2}{3}, \frac{3}{4}, \frac{5}{6}, \dots$
 ii) Improper fractions : Fractions greater than 1, i.e. $\frac{3}{2}, \frac{4}{3}, \frac{5}{2}, \dots$
7. i) L.C.M. of the fractions = L.C.M. of the numerators/H.C.F. of the denominators.
 ii) H.C.F. of the fractions = H.C.F. of the numerators/L.C.M. of the denominators.
8. $x\% = \frac{x}{100}$, $\frac{x}{y} = \left(\frac{100x}{y}\right)\%$
9. i) Simple Interest = Principal \times Time in years \times Annual Rate/100 = $\frac{PTR}{100}$.
 ii) Amount = Principal + Interest
10. i) Velocity or speed = Distance \div Time
 ii) Distance = Velocity \times Time
 iii) Relative Speed of a boat downstream = Speed of boat + Speed of current
 iv) Relative speed of a boat upstream = Speed of boat - Speed of current
11. i) Simple Average = Sum of the quantities \div No. of quantities
 ii) Weighted Average = $f_1x_1 + f_2x_2 + f_3x_3, \dots \div f_1 + f_2 + f_3, \dots$
12. i) Profit % = $\frac{\text{Profit}}{\text{C.P.}} \times 100$ ii) Loss % = $\frac{\text{Loss}}{\text{C.P.}} \times 100$
 iii) On Profit, SP = CP + Profit iv) On Loss, SP = CP - Loss
 v) S.P. at a profit of $x\% = CP + CP \times \frac{x}{100}$
 vi) S.P. at a loss of $x\% = C.P. - C.P. \times \frac{x}{100}$
13. Compound Interest : i) $A = P \left[1 + \frac{r}{100}\right]^n$, $n =$ No. of years, $r =$ rate, $A =$ Amount.
 ii) When rates for successive years are different, $A = P \left(1 + \frac{r_1}{100}\right) \left(1 + \frac{r_2}{100}\right) \dots$
 iii) When Int. is compounded $\frac{1}{2}$ yearly, $A = P \left[1 + \frac{r}{2 \times 100}\right]^{n \times 2}$.
 iv) For $n\%$ depreciation, Value after n yrs = Present Value $\left(1 - \frac{r}{100}\right)^n$

FORMULAE : ALGEBRA

1. $(a+b)^2 = a^2 + 2ab + b^2$, $a^2 + b^2 = (a+b)^2 - 2ab$
2. $(a-b)^2 = a^2 - 2ab + b^2$; $a^2 + b^2 = (a-b)^2 + 2ab$
3. (i) $(a+b)^2 = (a-b)^2 + 4ab$ (ii) $(a-b)^2 = (a+b)^2 - 4ab$
 (iii) $4ab = (a+b)^2 - (a-b)^2$ (iv) $ab = \frac{(a+b)^2 - (a-b)^2}{4}$
4. (i) $(a+b+c)^2 = a^2 + b^2 + c^2 + 2ab + 2bc + 2ca$ (v) $(a+b)^2 + (a-b)^2 = 2(a^2 + b^2)$
 (ii) $a^2 + b^2 + c^2 = \frac{(a+b+c)^2 - 2(ab+bc+ca)}{2}$
 (iii) $ab + bc + ca = \frac{(a+b+c)^2 - (a^2 + b^2 + c^2)}{2}$
5. $a^2 + b^2 + c^2 - ab - bc - ca = \frac{1}{2} \{ (a-b)^2 + (b-c)^2 + (c-a)^2 \}$
6. (i) $(a+b)^3 = a^3 + 3a^2b + 3ab^2 + b^3 = a^3 + b^3 + 3ab(a+b)$
 (ii) $a^3 + b^3 = (a+b)^3 - 3ab(a+b)$
7. (i) $(a-b)^3 = a^3 - 3a^2b + 3ab^2 - b^3 = a^3 - b^3 - 3ab(a-b)$
 (ii) $a^3 - b^3 = (a-b)^3 + 3ab(a-b)$
8. (i) $(a+b+c)^3 = a^3 + b^3 + c^3 + 3(a+b)(b+c)(c+a)$
 (ii) $a^3 + b^3 + c^3 = (a+b+c)^3 - 3(a+b)(b+c)(c+a)$
9. (i) $a^2 - b^2 = (a+b)(a-b)$ (iii) $a^3 + b^3 = (a+b)(a^2 - ab + b^2)$
 (ii) $a^2 + b^2 = \frac{(a+b)^2 + (a-b)^2}{2}$ (iv) $a^3 - b^3 = (a-b)(a^2 + ab + b^2)$
 (v) $a^3 + b^3 + c^3 - 3abc = (a+b+c)(a^2 + b^2 + c^2 - ab - bc - ca)$
 $= \frac{1}{2} (a+b+c) \{ (a-b)^2 + (b-c)^2 + (c-a)^2 \}$
10. (i) $-(b-c)(c-a)(a-b) = a^2(b-c) + b^2(c-a) + c^2(a-b)$
 $= bc(b-c) + ca(c-a) + ab(a-b)$
 $= a(b^2 - c^2) + b(c^2 - a^2) + c(a^2 - b^2)$
 (ii) $(b+c)(c+a)(a+b) = a^2(b+c) + b^2(c+a) + c^2(a+b) + 2abc$
 $= bc(b+c) + ca(c+a) + ab(a+b) + 2abc$
 $= a(b^2 + c^2) + b(c^2 + a^2) + c(a^2 + b^2) + 2abc$
 $= (a+b+c)(ab + bc + ca) - abc$
 (iii) $(a+b+c)(ab + bc + ca) = a^2(b+c) + b^2(c+a) + c^2(a+b) + 3abc$
 $= bc(b+c) + ca(c+a) + ab(a+b) + 3abc$
 $= a(b^2 + c^2) + b(c^2 + a^2) + c(a^2 + b^2) + 3abc$
 $= (b+c)(c+a)(a+b) + abc$
11. (i) $a^m \times a^n = a^{m+n}$ (iii) $a^m + a^n = a^{m-n}$
 (ii) $(a^m)^n = a^{mn}$ (iv) $a^0 = 1$ (When $a \neq 0$)
 (v) $a^{-n} = \frac{1}{a^n}$ (vi) $(ab)^m = a^m \cdot b^m$
 (vii) $\sqrt[n]{a} = a^{1/n}$ (viii) $\sqrt[n]{a} = a^{1/n}$
 (ix) $\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$ (x) $\sqrt[n]{a^m} = a^{m/n}$

12. i) Equation of a straight line $\rightarrow ax+by+c=0$

ii) Equation of the x-axis is $y=0$

iii) Equation of the y-axis is $x=0$

iv) Eqn. of a st. line parallel to x-axis is $y=a$

v) Eqn. of a st. line parallel to y-axis is $x=a$

13. i) General form of quadratic equation is $ax^2+bx+c=0$, where $a \neq 0$

ii) The roots of the quadratic eqn. $x = \frac{-b \pm \sqrt{b^2-4ac}}{2a}$, two in number.

iii) Nature of the roots ; -

a) Roots are Real and Equal if $b^2-4ac=0$ i.e. $b^2=4ac$.

b) Roots are Real but Unequal if b^2-4ac is positive.

c) Roots are Real and Rational if b^2-4ac is a perfect square.

d) Roots are Real and Irrational if b^2-4ac is not a perfect square.

e) Roots are Imaginary if b^2-4ac is negative.

14. If $a:b::c:d$, then

(i) $ad=bc$ Cross-multiplied (ii) $b/a=d/c$... Invertendo.

(iii) $a/c=b/d$... Alternando. (iv) $\frac{a+b}{b} = \frac{c+d}{d}$... Componendo.

(v) $\frac{a-b}{b} = \frac{c-d}{d}$... Dividendo. (vi) $\frac{a}{a-b} = \frac{c}{c-d}$... Convertendo.

(vii) $\frac{a+b}{a-b} = \frac{c+d}{c-d}$... Componendo and Dividendo.

15. If $a:b::b:d$, i.e. in Continued proportion

(i) $a/b = b/c$ i.e. $b^2=ac$

(ii) $a/c = a^2/b^2$

16. If $a:b::c:d$, i.e. $a/b = c/d$

i) Each ratio $= \frac{a+c}{b+d} = \frac{a+c+e+g...}{b+d+f+h...}$ (Addendo)

ii) Each ratio $= \frac{a-c}{b-d}$

17. Logarithms : $a^m=b \Rightarrow \log_a b = m$, $a > 0$ and $a \neq 1$

i) $\log_a 1 = 0$, $\log_a a = 1$ ii) $\log_a m^n = n \log_a m$

iii) $\log_a mn = \log_a m + \log_a n$ iv) $\log_a \frac{m}{n} = \log_a m - \log_a n$

v) $\log_m m \times \log_m m = 1$

18. Commutative law \rightarrow a) $x+y=y+x$ b) $xy=yx$

Associative Law \rightarrow a) $(x+y)+z=x+(y+z)$ b) $(xy)z=x(yz)$

Additive Identity $\rightarrow x+0=x=0+x$; Distributive Law \rightarrow

Multiplicative Identity $\rightarrow x \times 1 = x = 1 \times x$ $x(y \pm z) = xy \pm xz$

Additive Inverse $\rightarrow x + (-x) = 0 = (-x) + x$

FORMULAE : MENSURATION

5

15/11/20

1. i) Area of a Triangle = $\frac{1}{2} \times \text{base} \times \text{altitude}$
 = $\sqrt{s(s-a)(s-b)(s-c)}$, where $s = \frac{a+b+c}{2}$ [Heron's formula]
 - ii) Area of an equilateral triangle = $\frac{\sqrt{3}}{4} a^2$, where $a = \text{side}$.
 - iii) Height of an equilateral triangle = $\frac{\sqrt{3}}{2} a$.
 - iv) In a right-angled triangle, $(\text{hypotenuse})^2 = (\text{Base})^2 + (\text{perpendicular})^2$
2. i) Area of the Rectangle = Length \times Breadth
 ii) Diagonal of the Rectangle = $\sqrt{l^2 + b^2}$
 iii) Perimeter of the Rectangle = $2(l+b)$
 - v) In Isosceles triangle = $\frac{1}{2} b \sqrt{a^2 - \frac{b^2}{4}}$
3. i) Area of a Square = a^2 , where $a = \text{side}$.
 ii) Diagonal of a Square = $a\sqrt{2}$
 iii) Perimeter of a Square = $4a$
4. i) Area of a Rhombus = $\frac{1}{2}$ (Product of two diagonals)
 ii) Area of a Parallelogram = Base \times Height
 iii) Area of a Trapezium = $\frac{1}{2} \times (\text{Sum of two parallel sides}) \times \text{Height}$
 iv) Area of the four walls of a room = $2(l+b)h$.
5. i) Area of the circle = πr^2 , $r = \text{radius}$.
 ii) Perimeter/Circumference of the circle = $2\pi r$.
 iii) Area of the circular ring = $\pi(R^2 - r^2)$. $R = \text{Outer radius}$.
 iv) Circumference of the circular ring = $2\pi(R-r)$.
6. i) Total surface area of the cuboid = $2(ab + bc + ca)$, Sides - a, b, c
 ii) Volume of the cuboid = abc
 iii) Diagonal of the rectangular parallelepiped = $\sqrt{a^2 + b^2 + c^2}$
7. i) Total surface area of the cube = $6a^2$; Side - a
 ii) Volume of the cube = a^3
 iii) Diagonal of the cube = $a\sqrt{3}$
8. i) Volume of a cylinder = $\pi r^2 h$; Radius - r , height - h
 ii) Area of the curved surface of a cylinder = $2\pi rh$
 iii) Total surface area of a cylinder = $2\pi r(h+r)$
 iv) Volume of a hollow cylinder = $\pi(R^2 - r^2)h$
9. i) Volume of the sphere = $\frac{4}{3} \pi r^3$
 ii) Total surface area of the sphere = $4\pi r^2$
 iii) Volume of the hemisphere = $\frac{2}{3} \pi r^3$
 iv) Surface area of the hemisphere = $3\pi r^2$

TRIGONOMETRY

7

Admth.

1. Some People Have,
Curling Brown Hair,
They are Proud and Brave.

$$\sin \theta = \frac{P}{H} = \frac{\text{Perp}}{\text{Hyp.}}$$

$$\cos \theta = \frac{B}{H} = \frac{\text{Base}}{\text{Hyp.}}$$

$$\tan \theta = \frac{P}{B} = \frac{\text{Perp}}{\text{Base}}$$

$$\text{Cosec } \theta = \frac{\text{Hyp}}{\text{Perp}} = \frac{H}{P}$$

$$\text{Sec } \theta = \frac{\text{Hyp}}{\text{Base}} = \frac{H}{B}$$

$$\text{Cot } \theta = \frac{\text{Base}}{\text{Perp}} = \frac{B}{P}$$

2. i) A Radian, $1^\circ = 57^\circ 17' 44.8''$ (nearly)

ii) $\pi^\circ = \pi$ Radian $= 180^\circ$

3. i) $\sin \theta = 1/\text{Cosec } \theta$

ii) $\text{Cosec } \theta = 1/\sin \theta$

ix) $\tan \theta = \frac{\sin \theta}{\cos \theta}$

iii) $\cos \theta = 1/\text{Sec } \theta$

iv) $\text{Sec } \theta = 1/\cos \theta$

x) $\text{Cot } \theta = \frac{\cos \theta}{\sin \theta}$

v) $\tan \theta = 1/\text{Cot } \theta$

vi) $\text{Cot } \theta = 1/\tan \theta$

vii) $\sin^2 \theta + \cos^2 \theta = 1$

viii) $\text{Sec}^2 \theta = 1 + \tan^2 \theta$

ix) $\text{Cosec}^2 \theta = 1 + \cot^2 \theta$

4. ANGLES \rightarrow	0°	30°	45°	60°	90°
\sin —	0	$1/2$	$1/\sqrt{2}$	$\sqrt{3}/2$	1
\cos —	1	$\sqrt{3}/2$	$1/\sqrt{2}$	$1/2$	0
\tan —	0	$1/\sqrt{3}$	1	$\sqrt{3}$	∞

5. i) $\sin(90^\circ - \theta) = \cos \theta$

ii) $\cos(90^\circ - \theta) = \sin \theta$

iii) $\text{Cosec}(90^\circ - \theta) = \sec \theta$

iv) $\sec(90^\circ - \theta) = \text{Cosec } \theta$

v) $\tan(90^\circ - \theta) = \cot \theta$

vi) $\cot(90^\circ - \theta) = \tan \theta$

6. i) $\sin(90^\circ + \theta) = \cos \theta$

ii) $\cos(90^\circ + \theta) = -\sin \theta$

iii) $\text{Cosec}(90^\circ + \theta) = \sec \theta$

iv) $\sec(90^\circ + \theta) = -\text{Cosec } \theta$

v) $\tan(90^\circ + \theta) = -\cot \theta$

vi) $\cot(90^\circ + \theta) = -\tan \theta$

7. i) $\sin(180^\circ - \theta) = \sin \theta$

ii) $\cos(180^\circ - \theta) = -\cos \theta$

iii) $\text{Cosec}(180^\circ - \theta) = \text{Cosec } \theta$

iv) $\sec(180^\circ - \theta) = -\sec \theta$

v) $\tan(180^\circ - \theta) = -\tan \theta$

vi) $\cot(180^\circ - \theta) = -\cot \theta$

\sin^+	All^+
\tan^+	\cos^+

8. From Pythagoras theorem,

$3^2 + 4^2 = 5^2$ And its multiples, like—

$6^2 + 8^2 = 10^2$

$9^2 + 12^2 = 15^2$ and so on, are Pythagorean triples.

$5^2 + 12^2 = 13^2$

$8^2 + 15^2 = 17^2$

$24^2 + 10^2 = 26^2$

$15^2 + 20^2 = 25^2$

$1^3 = 1$

$9^3 = 729$

$2^3 = 8$

$10^3 = 1000$

$3^3 = 27$

$11^3 = 1331$

$4^3 = 64$

$12^3 = 1728$

$5^3 = 125$

$15^3 = 3375$

$6^3 = 216$

$7^3 = 343$

$8^3 = 512$

- The distance between two given points (x_1, y_1) and (x_2, y_2)

$$= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$
- The distance of any point (x, y) from origin $(0, 0)$

$$= \sqrt{x^2 + y^2}$$
- The co-ordinates of a point $P(x, y)$ which divides the line joining points (x_1, y_1) and (x_2, y_2) in ratio $m:n$;

$$P_x = \frac{mx_2 + nx_1}{m+n}$$
 Externally; $P_x = \frac{mx_2 - nx_1}{m-n}$
 Internally $P_y = \frac{my_2 + ny_1}{m+n}$ Externally; $P_y = \frac{my_2 - ny_1}{m-n}$
- The co-ordinates of the mid-point of the line joining points (x_1, y_1) and (x_2, y_2)

$$P(x, y) = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$
- The co-ordinates of the Centroid of ΔABC having vertices $A(x_1, y_1)$, $B(x_2, y_2)$ and $C(x_3, y_3)$;

$$G(x, y) = \left(\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3} \right)$$
- Slope (Gradient) = Vertical rise / horizontal distance
 - Slope $m = \tan \theta$; if inclination is θ .
 - Slope of x -axis, $m = \tan 0^\circ = 0$
 - Slope of y -axis, $m = \tan 90^\circ = \infty$
 - Slope is +ve, when it makes an acute angle in anticlockwise direction.
 - Slope is -ve, when it makes an acute angle in clockwise direction.
 - Slope of a line passing through (x_1, y_1) and (x_2, y_2)

$$m = \tan \theta = \frac{y_2 - y_1}{x_2 - x_1}$$
 - For Parallel lines, $m_1 = m_2$ i.e. slopes are equal.
 - For Perpendicular lines, $m_1 \cdot m_2 = -1$
 - Slope of every line parallel to x -axis is zero.
- If three points A, B and C are collinear, then Slope of $AB =$ Slope of BC .
- Equation of a line:
 - $y = mx + c$ [Slope-Intercept form]
 - $y - y_1 = m(x - x_1)$ [Point (given) - Slope form]
 - $m = \frac{y_2 - y_1}{x_2 - x_1}$ [Two-points form; then to use eqn. no. ii]
 - Equation of x -axis is $y = 0$
 - Equation of y -axis is $x = 0$
 - Eqn. of a line parallel to x -axis at a distance 'a' from it is $y = a$
 - Eqn. of a line parallel to y -axis at a distance 'b' from it is $x = b$

LOGARITHM

$$1. a^n = b \Rightarrow \log_a b = n$$

[$a > 0, a \neq 1$]

$$2. \log_a 1 = 0, \log_a a = 1$$

$$3. \log_a mn = \log_a m + \log_a n$$

$$4. \log_a \frac{m}{n} = \log_a m - \log_a n$$

$$5. \log_a m^n = n \log_a m$$

$$6. a^{\log_a x} = x$$

$$7. \log_a m = \log_b m \times \log_a b$$

$$8. \log_b m = \frac{\log_a m}{\log_a b} \quad \left[\begin{array}{l} m > 0 \\ a, b > 0 \\ a \neq 1, b \neq 1 \end{array} \right]$$

$$9. \log_b a \times \log_a b = 1$$

$$10. \log_b a = \frac{1}{\log_a b}$$

$$11. \text{If } \log_a x = \log_a y \Rightarrow x = y$$

MENSURATION

$$1. \text{Area of a Sector} = \pi r^2 \times \frac{\theta}{360}$$

$$2. \text{Perimeter of a Sector} = 2r + 2\pi r \times \frac{\theta}{360}$$

$$3. \text{Radius of Incircle, } r = \frac{\pi r^2}{s} \quad [s = \frac{a+b+c}{2}]$$

For Equilateral Triangle,

$$r = \frac{1}{3} \cdot \frac{\sqrt{3}}{2} a = \frac{\sqrt{3}}{6} a$$

$$4. \text{Radius of circumcircle, } R = \frac{abc}{4\pi r^2}$$

For Equilateral Triangle,

$$R = \frac{2}{3} \cdot h \Rightarrow \frac{2}{3} \cdot \frac{\sqrt{3}}{2} a \Rightarrow \frac{\sqrt{3}}{3} a$$

$$\therefore R = 2r$$

STATISTICS

Arithmetic Mean: -

$$i) \text{ Direct Method: } \bar{x} = \frac{\sum fx}{N}$$

Where, x = Mid Value of class interval
 f = frequency of class interval
 $N = \sum f$, total frequency

ii) Short Cut Method:

$$\bar{x} = A + \frac{\sum fd}{N}$$

Where, A = Assumed Mean
 $d = x - A$

iii) Step Deviation Method:

$$\bar{x} = A + \frac{\sum fu \times i}{N}$$

Where, i = Length of class interval
 $u = \frac{x - A}{i}$

Median:

i) For Ungrouped data -

When N is odd, Median = $\frac{N+1}{2}$ th figure serially

When N is even, Median = $\frac{1}{2} \left[\frac{N}{2} \text{th. term} + \frac{N}{2} + 1 \text{th. term} \right]$

ii) For Grouped data -

$$\text{Median} = l + \frac{\frac{N}{2} - F}{f_m} \times i$$

$$\text{iii) Mode} = l + \frac{f_m - f_1}{2f_m - f_1 - f_2} \times i$$

Where, l = Lower class boundary of the modal class

f_m = Frequency of the modal class

f_1 = Frequency just preceding the modal class

f_2 = Frequency just succeeding the modal class

i = Length/Width of the modal class

$$\text{iv) Mean - Mode} = 3(\text{Mean} - \text{Median})$$

Where, l = Lower class boundary of the median class

N = Total frequency

F = Cumulative frequency, preceding to median class

f_m = Frequency of the median class

i = Length of the median class.

ARITHMETIC PROGRESSION

First term = a , Common Difference = d , Sum = S

$$\text{i) } n\text{-th term, } t_n = a + (n-1)d \quad \text{ii) } S_n = \frac{n}{2}(a+l)$$

$$a_m - a_n = (m-n)d$$

$$= \frac{n}{2} \{2a + (n-1)d\}$$

$$\text{iii) Sum of the first } n \text{ natural nos.} = 1 + 2 + 3 + 4 + \dots + n$$

$$= \frac{n(n+1)}{2}$$

$$\text{iv) } n\text{-th term from the end} = a + (m-n)d = l - (n-1)d$$

GEOMETRICAL PROGRESSION

a, ar, ar^2, \dots First term = a , Common ratio = r

$$\text{i) } n\text{-th term, } a_n = ar^{n-1}$$

$$\text{ii) } n\text{-th term from the end of G.P. having } m \text{ terms} = ar^{m-n}$$

$$\text{iii) } n\text{-th term from the end having last term } l = l \left(\frac{1}{r}\right)^{n-1}$$

$$\text{iv) } \text{If } |r| < 1, S_n = a \frac{1-r^n}{1-r}$$

$$\text{If } r \leq -1 \text{ or } r > 1, S_n = a \frac{r^n - 1}{r - 1}$$

$$\text{If } r = 1, S_n = na$$

$$\text{v) } \text{If } l = \text{last term, } l = ar^{n-1}$$

$$S_n = \frac{a - lr}{1-r} = \frac{lr - a}{r-1}$$