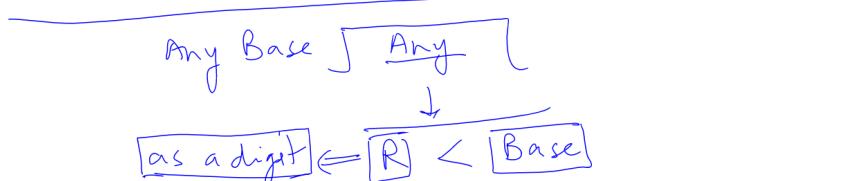
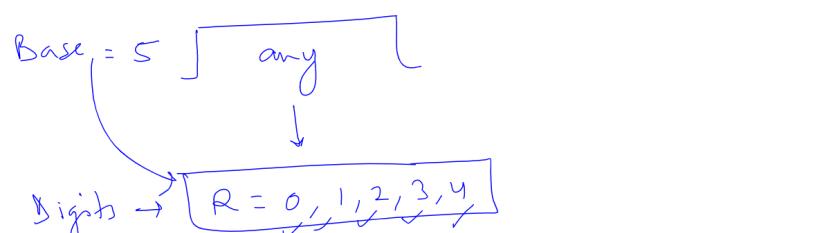
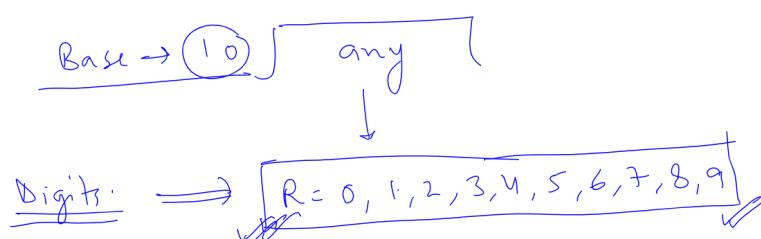
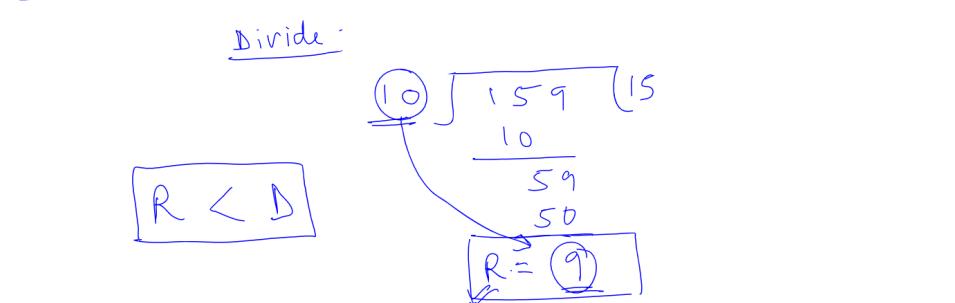
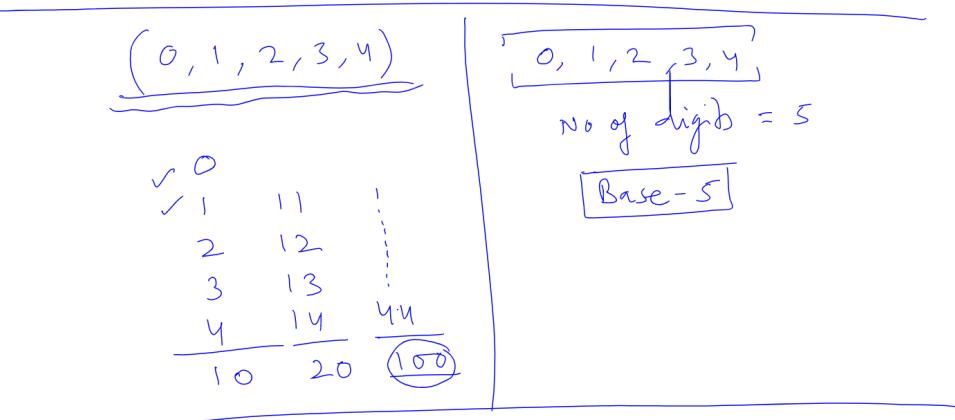
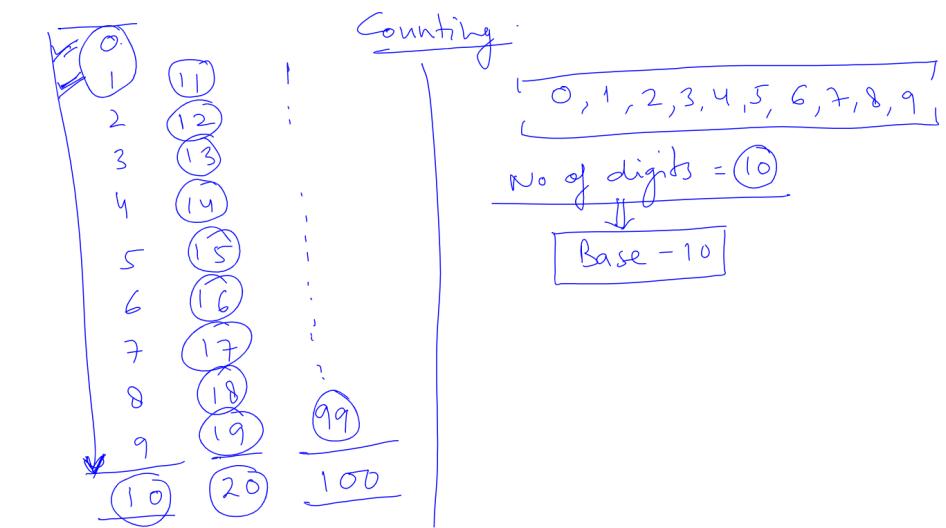


Notes from the class titled

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# Xie-1-Quant-Speed Maths-1



$$\begin{array}{c|c}
 (0-9)_{10} & (0-4)_5 \\
 \hline
 (0-7)_8 & (0-6)_7 \\
 \hline
 (0-8)_9 & (0-3)_4
 \end{array}$$

Add:

$$\begin{array}{r}
 1 \quad 8 \\
 + 1 \quad 9 \\
 \hline
 \textcircled{1} \quad 7
 \end{array}$$

(Process is wrong)

Shortcut

Ans  $\rightarrow (3 \quad 7)$

$$\begin{array}{r}
 (1 \quad 8)_{10} \\
 (1 \quad 9)_{10} \\
 \hline
 (3 \quad 7)_{10}
 \end{array}$$

Carry over

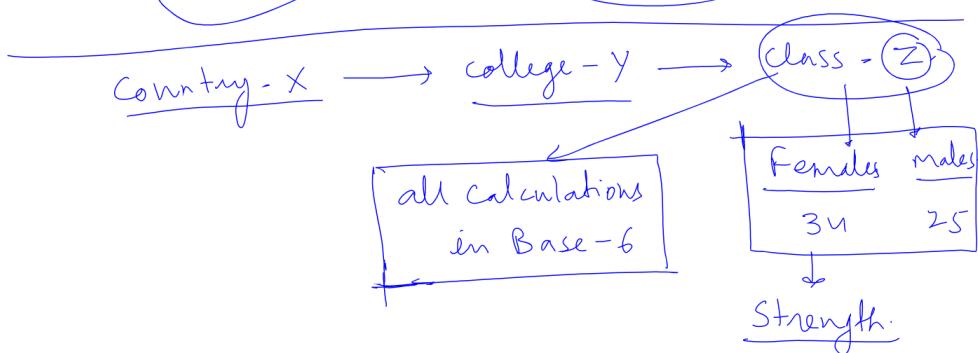
$10 \sqrt{17} \quad \textcircled{1} \text{ Quotient}$

$\frac{10}{R = 7}$

$$\begin{array}{r}
 6 \sqrt{6} \quad \textcircled{1} \\
 \frac{6}{R = 0}
 \end{array}$$

$$\begin{array}{r}
 (3 \quad 4)_6 \\
 (2 \quad 5)_6 \\
 \hline
 (1 \quad 0 \quad 3)_6
 \end{array}$$

$$\begin{array}{r}
 6 \sqrt{9} \quad \textcircled{1} \\
 \frac{6}{R = 3}
 \end{array}$$



$$\begin{array}{r}
 \begin{array}{r}
 (2 \ 6 \ 7)_8 \\
 + (3 \ 4 \ 3)_8 \\
 \hline
 (6 \ 3 \ 2)_8
 \end{array}
 \end{array}
 \quad
 \left\{
 \begin{array}{l}
 G \rightarrow 632 \checkmark \\
 N \rightarrow 632 \checkmark \\
 S \rightarrow 632 \checkmark \\
 H \rightarrow 632 \checkmark \\
 A \rightarrow 632 \checkmark
 \end{array}
 \right.$$

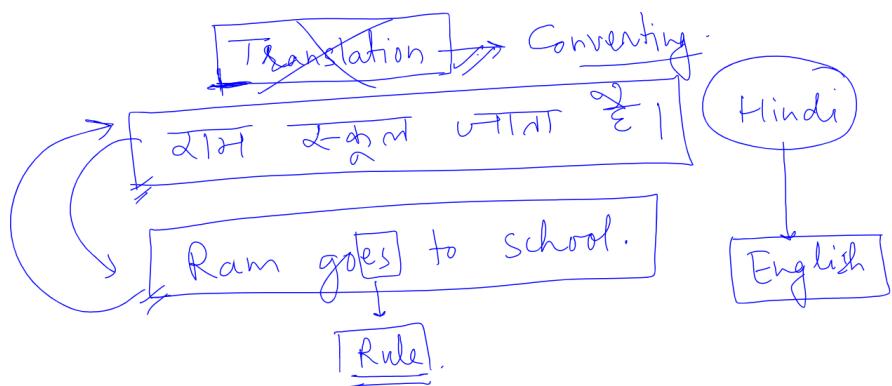
$$\begin{array}{r}
 (1 \ 8)_{10} \\
 + (1 \ 9)_{10} \\
 \hline
 (3 \ 7)_{10}
 \end{array}
 \quad
 \begin{array}{r}
 (3 \ 7)_{10} \\
 - (1 \ 9)_{10} \\
 \hline
 (1 \ 8)_{10}
 \end{array}$$

Subtraction  $-1 \text{ Base} = 10$

$$\begin{array}{r}
 (3 \ 2)_{10} \\
 - (1 \ 7)_{10} \\
 \hline
 (1 \ 9)_{10}
 \end{array}$$

$$\begin{array}{r}
 (1 \ 0)_{10} \\
 - (1 \ 3)_{10} \\
 \hline
 (0 \ 7)_{10}
 \end{array}
 \quad
 \begin{array}{r}
 (0 \ 7)_{10} \\
 + (3 \ 4)_{10} \\
 \hline
 (0 \ 2 \ 5)_{10}
 \end{array}$$

$$\begin{array}{r}
 (2 \ 6 \ 7)_8 \\
 + (3 \ 4 \ 3)_8 \\
 \hline
 (6 \ 3 \ 2)_8
 \end{array}
 \quad
 \begin{array}{r}
 (6 \ 3 \ 2)_8 \\
 - (2 \ 6 \ 7)_8 \\
 \hline
 (3 \ 4 \ 3)_8
 \end{array}$$



$$(123)_5 \leftarrow \text{Base-5}$$

$$(?)_{10} \leftarrow \text{Base-10}$$

Place-Values:

H's    Tens    unit  
1    2    3

$$\begin{aligned} 3 \times 1 &= 3 \\ 2 \times 10 &= 20 \\ 1 \times 100 &= 100 \end{aligned}$$

This place  $(123)_{10}$   
Always Base-10

$$\begin{aligned} (2110) & \\ (123)_{10} & \leftarrow 10 \\ 3 \times 10^0 &= 3 \\ 2 \times 10^1 &= 20 \\ 1 \times 10^2 &= 100 \\ \hline (123)_{10} & \end{aligned}$$

Switch:

$$\begin{aligned} (123)_5 & \leftarrow 5 \\ 3 \times 5^0 &= 3 \\ 2 \times 5^1 &= 10 \\ 1 \times 5^2 &= 25 \\ \hline (38)_{10} & \end{aligned}$$

$$(123)_6 \rightarrow (?)_{10}$$

$$\begin{array}{c}
 (1 \ 2 \ 3) \ 6 \\
 \downarrow \quad \downarrow \quad \downarrow \\
 3 \times 6 = 3 \\
 2 \times 6 = 12 \\
 1 \times 6 = 36 \\
 \hline
 (51)_{10}
 \end{array}$$

$$\begin{array}{c}
 \begin{array}{|c|c|c|} \hline
 S & 38 & R=3 \\ \hline
 S & Q=7 & R=2 \\ \hline
 S & Q=1 & R=1 \\ \hline
 \end{array} \quad (123)_5 \longrightarrow (38)_{10} \\
 \begin{array}{|c|c|c|} \hline
 S & 38 & R=3 \\ \hline
 S & Q=7 & R=2 \\ \hline
 S & Q=1 & R=1 \\ \hline
 \end{array} \quad (38)_{10} \longrightarrow (123) \boxed{5} \\
 \begin{array}{|c|c|c|} \hline
 S & 51 & R=3 \\ \hline
 S & Q=8 & R=2 \\ \hline
 S & Q=1 & R=1 \\ \hline
 \end{array} \quad (51)_{10} \longrightarrow (123)_6
 \end{array}$$

$$\begin{array}{|c|c|c|} \hline
 S & 51 & R=3 \\ \hline
 S & Q=8 & R=2 \\ \hline
 S & Q=1 & R=1 \\ \hline
 \end{array} \quad 6 \overline{)110} \quad R=1$$

$$(167)_{10} \longrightarrow (247)_8$$

$$\begin{array}{c}
 \boxed{8 \overline{)167} \quad (20) \quad 8 \overline{)20} \quad (2) \quad 8 \overline{)27} \quad (0) \\
 \downarrow \quad \downarrow \quad \downarrow \\
 \begin{array}{c} 160 \\ \hline R=7 \end{array} \quad \begin{array}{c} 16 \\ \hline R=4 \end{array} \quad \begin{array}{c} 27 \\ \hline R=2 \end{array}
 \end{array}$$

Summary: Base - System

Add / Sub / Convert

Base - 10

10  $\xrightarrow{1}$  exactly one digit per step

Base - 100

10  $\xrightarrow{2}$  exactly two digits per step

Base - 1000

10  $\xrightarrow{3}$  exactly three digits per step

$$\overline{(18)}_{10}$$

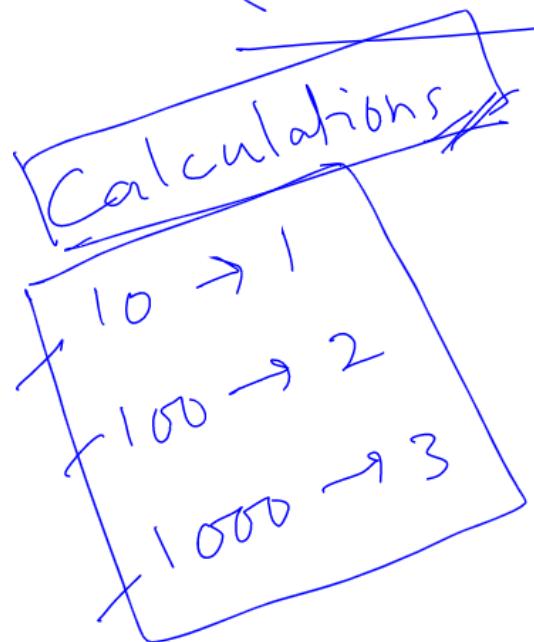
$$(18)_{100}$$

$$\overline{(19)}_{10}$$

$$(19)_{100}$$

$$\overline{(37)}_{10}$$

$$\overline{(0217)}_{100}$$



$$(18)_{1000}$$

$$(19)_{1000}$$

$$\overline{(002017)}_{1000}$$