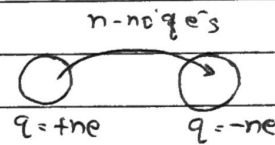
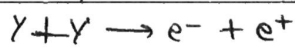


Ch-01 Electrostatics

- **Electric charge :** $1C = 2.5 \times 10^9 \text{ esu of charge}$
- Charge is an intrinsic property of matter which gives rise to electric force b/w various objects.
- Symbol $\rightarrow q$ or Q
- SI Unit $\rightarrow$ Coulomb (C) Dimension, $Q = I \times t$
Scalar Quantity $= [AT]$
- Types of Charge $\rightarrow$ +ve and -ve.
- Like charges repel each other and unlike charges attract each other.

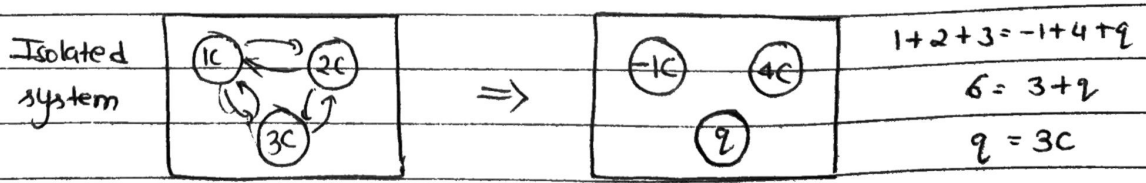
Property of Charge

- 1) charge is transferable. 
- 2) Charge is associated with mass.
(No charge can exist without mass.)
- 3) charge is invariant (do not vary with speed of body).
{ Mass increases with velocity }
- 4) Conservation of charge : Charge can neither be created, nor destroyed but only be transferred from one body to another. { Pair production in charge but net charge 0 }



OR

The total charge of an isolated system remains constant.



Quantisation of chargeQuantisation $\rightarrow$ Available in fixed amount.

- i) The smallest charge which exists independently is charge on electron.

$$1e^- = 1.6 \times 10^{-19} \text{ C} \quad (\text{fundamental charge})$$

- ii) Charge always exist in Integral multiple of fundamental charge.

$$1e^-, 2e^-, 3e^-, 4e^- \dots n e^-$$

$$-1e^-, -2e^-, -3e^-, -4e^-, \dots -n e^-$$

$$Q = \pm n e^-$$

$\downarrow$ charge $\downarrow$ Integer

Charge on e^-

- Q- Can a charge $8 \times 10^{-19} \text{ C}$ be given to a body?

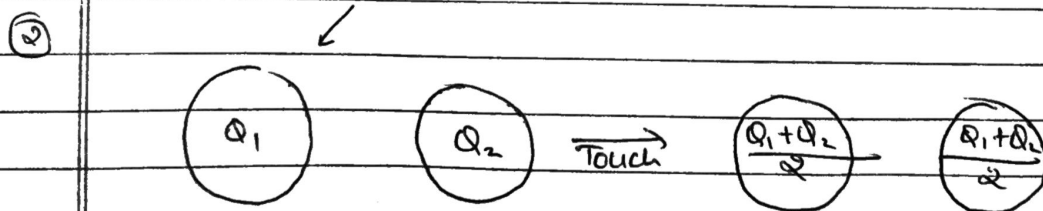
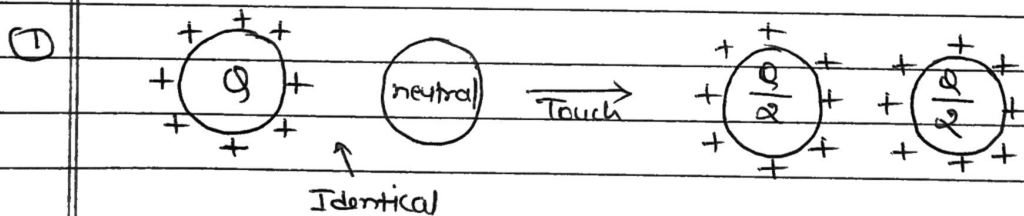
$$Q = \pm n e$$

$$8 \times 10^{-19} = n \times 1.6 \times 10^{-19}$$

$$n = \frac{80}{16} = 5 \quad (\text{integer}) \quad \therefore \text{Given charge exists}$$

Methods of Charging

- 1) charging by conduction $\hat{=}$ Direct contact.



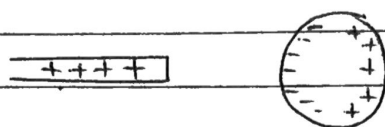
• charging by friction :-

⇒ Glass Rod + silk cloth → Glass rod (+ve charge) + silk cloth (-ve charge)

⇒ Ebonite rod + Animal fur (wool) → Ebonite rod (-ve charge) + Animal fur (+ve charge)

Page No.				
Date				

2) Charging by Induction : without contact.



nearer end → opp. charge

farther end → same charge

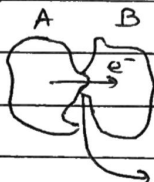
overall charge = 0.

3) Charging by Friction

If n e^- s transfers from A to B

A : $q = +ne$

B : $q = -ne$



Rubbing → Thermal Energy →

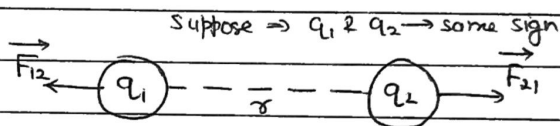
some outer e^- falls from one body to another

Coulomb's Law

1) $\vec{F}_{12} = -\vec{F}_{21}$

2) $F = \frac{kq_1q_2}{r^2}$ without sign

↳ direct decide



Suppose $\Rightarrow q_1 \& q_2 \rightarrow$ same sign

3) $k = \frac{1}{4\pi\epsilon}$ $\epsilon \rightarrow$ permittivity of medium.

$\epsilon \uparrow \Rightarrow k \downarrow \Rightarrow F \downarrow$

4) for air / free space / vacuum

$k = \frac{1}{4\pi\epsilon_0}$

$\epsilon_0 \rightarrow$ absolute permittivity

↳ minimum value of ϵ

$\epsilon \rightarrow$ min $\rightarrow$ air / vacuum

$\Rightarrow F \rightarrow$ maximum in air

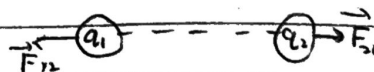
$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{Nm}^2$

air / vacuum

$k = 9 \times 10^9 \text{ Nm}^2/\text{C}^2$

$F \rightarrow$ max in air / vacuum

5) F acts along line joining two charge.
(central force)



NOTE:

Repulsion is sure test of electrification.

It means if two objects repel each other then they must be charged objects.

Page No. _____

Date _____

6) Coulomb's law valid for point charge only.

7) Coulomb's law valid for stationary charges.

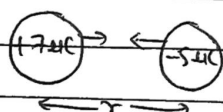
8) F follows inverse square law $F \propto \frac{1}{r^2}$

9) ~~work done~~ Electrostatic force is a conservative force

- work done depends only on initial & final position & do not depend on path.
- work done in a round trip by electrostatic force is zero.

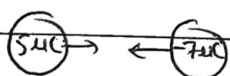
Q-1) The charges on two spheres are $+7\mu C$ and $-5\mu C$, resp. They experience a force F . If each of them is given an additional charge of $-2\mu C$, then new force attraction will be

- (a) F (b) $F/2$
(c) $F/\sqrt{3}$ (d) $2F$



$$F = k \frac{(7)(5)}{r^2} = \frac{35k}{r^2}$$

$-2\mu C$ given to each.



$$F' = k \frac{(5)(7)}{r^2} = \frac{35k}{r^2} = F$$

Q-2) A charge Q is divided into two parts such that the electrostatic force between two parts is maximum. Find the charge on each part.

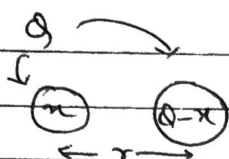
- a) $\frac{Q}{4}, \frac{3Q}{4}$ (c) $\frac{Q}{5}, \frac{4Q}{5}$

- ~~b) $\frac{Q}{2}, \frac{Q}{2}$~~

- (d) $\frac{Q}{3}, \frac{2Q}{3}$

Xdd
akher

Aadha Aadha time for us force maximum hoti hai!



$$F = \frac{k(Q-x)x}{r^2}$$

$F \rightarrow$ Maxima

$y \rightarrow$ Maximum, $\frac{dy}{dx} = 0$

$F \rightarrow$ Maximum, $\frac{dF}{dx} = 0$

$$\frac{d}{dx} \frac{k(Q-x)x}{r^2} = 0$$

$$\frac{d[(Q-x)x]}{dx} = 0$$

$$\frac{d(Qx - x^2)}{dx} = 0$$

$$Q - 2x = 0$$

$$Q = 2x$$

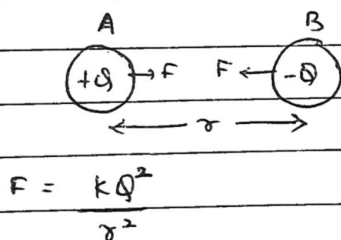
$$x = \frac{Q}{2}$$

Q- Two point charges A and B, having charges $+Q$ and $-Q$ resp, are placed at certain distance apart and force acting b/w them is F . If 25% charge of A is transferred to B, then force b/w the charges becomes :

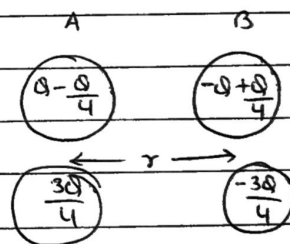
(A) $\frac{16F}{9}$ (b) $\frac{4F}{3}$

(C) F ~~(d) $\frac{9F}{16}$~~

NEET-19



$\Rightarrow$ 25% charge of A transfers to B



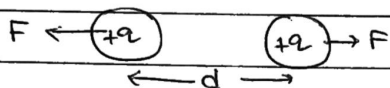
$$F' = \frac{k \left(\frac{3Q}{4} \right) \left(\frac{3Q}{4} \right)}{r^2}$$

$$= \frac{9 k Q^2}{16 r^2}$$

$$F' = \frac{9 F}{16}$$

- Q. Two positive ions, each carrying a charge q , are separated by a distance d . If F is the force of repulsion b/w the ions, the no. of electrons missing from each ion will be (e being the charge on an electron)

a) $\frac{4\pi\epsilon_0 Fd^2}{e^2}$ (b) $\sqrt{\frac{4\pi\epsilon_0 Fe^2}{d^2}}$ (2010)
c) $\sqrt{\frac{4\pi\epsilon_0 Fd^2}{e^2}}$ (d) $\frac{4\pi\epsilon_0 Fd^2}{q^2}$



$q = +ne$

$F = \frac{kq^2}{d^2}$

$F = \frac{1}{4\pi\epsilon_0} \frac{n^2 e^2}{d^2} \Rightarrow F \cdot 4\pi\epsilon_0 d^2 = n^2 e^2$

$\sqrt{\frac{4\pi\epsilon_0 Fd^2}{e^2}} = n$

Comparison with Law of Gravitation

$F_e = \frac{kq_1 q_2}{r^2}$

$F_g = \frac{Gm_1 m_2}{r^2}$

Similarity!

- both follows $F \propto \frac{1}{r^2}$ (inverse sq. law)
- Acts along line joining centres of bodies (central force)

Differences:

- G is universal constant.
 $G = 6.67 \times 10^{-11} \text{ Nm}^2/\text{kg}^2$
- K depends on medium
air/vacuum $K = 9 \times 10^9 \text{ Nm}^2/\text{C}^2$
- F_g is attractive only
- F_e can be attractive or repulsive.

Q- Find the ratio of electrostatic force to gravitational force b/w two electrons kept in free space.

$$|e| = 1.6 \times 10^{-19} \text{ C}$$

$$m_e = 9.1 \times 10^{-31} \text{ kg}$$

$$k = 9 \times 10^9 \text{ Nm}^2/\text{C}^2$$

$$G = 6.67 \times 10^{-11} \text{ Nm}^2/\text{kg}^2$$

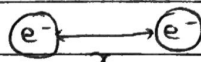
a) 10^{12}

b) 10^{24}

c) 10^{32}

~~d) 10^{42}~~

$$\frac{F_e}{F_g} = ?$$



$$\frac{F_e}{F_g} = \frac{kq_1q_2}{r^2} = \frac{9 \times 10^9 \times e^2}{6.67 \times 10^{-11} \times m^2}$$

$$= \frac{9 \times 10^9 \times (1.6 \times 10^{-19})^2}{6.67 \times 10^{-11} \times (9.1 \times 10^{-31})^2}$$

$$\approx 10^{42}$$

Q- Suppose the charge of a proton and an electron differ slightly. One of them is $-e$, the other is $(e + \Delta e)$. If the net of electrostatic force and gravitational force between two hydrogen atoms placed at a distance d (much greater than atomic size) apart is zero, then Δe is of the order of [Given mass of hydrogen $m_H = 1.67 \times 10^{-27} \text{ kg}$].

a) 10^{-23} C

~~b) 10^{-37} C~~

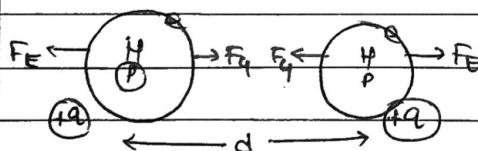
(20M)

c) 10^{-47} C

(d) 10^{-20} C

electron = $-e$

proton = $e + \Delta e$



Net charge on H-atom = $-e + e + \Delta e$

$$q = \Delta e$$

Given: net force is zero,

$$F_e = F_g$$

$$\frac{kq^2}{d^2} = \frac{Gm^2}{d^2}$$

$$9 \times 10^9 \times (\Delta e)^2 = 6.67 \times 10^{-11} \times (1.67 \times 10^{-27})^2$$

$$9 \times 10^9 \times (\Delta e)^2 = 6.67 \times 10^{-11} \times (1.67)^2 \times 10^{-54}$$

$$10^{10} \cdot (\Delta e)^2 = 6.67 \times (1.67)^2 \times 10^{-65}$$

$$(\Delta e)^2 \approx 6.67 \times (1.67)^2 \times 10^{-75}$$

$$\Delta e \approx 2.5 \times 1.67 \times 10^{-37.5}$$

$$9 \times 10^9 \times (\Delta e)^2 = 6.67 \times 10^{-11} \times (1.67 \times 10^{-27})^2$$

$$\boxed{\tan \theta \propto \frac{1}{mg}}$$

$$\Rightarrow \tan \theta \propto \frac{1}{mg}$$

max zyada
 θ kam

Page No. _____

Date _____

- Q- Two identical small charged spheres, each having a mass 'm', hang in equilibrium as shown. The length of each string is l , and the ~~magnitude~~ angle made by any string with the vertical is θ . Find the magnitude of charge on each sphere.

Equilibrium: Net force = 0

$$F_{\text{net } x} = 0$$

$$F_{\text{net } y} = 0$$

$$T \sin \theta = F_e \quad \text{--- (1)}$$

$$T \cos \theta = mg \quad \text{--- (2)}$$

$$\text{(1)} \div \text{(2)}$$

$$\tan \theta = \frac{F_e}{mg}$$

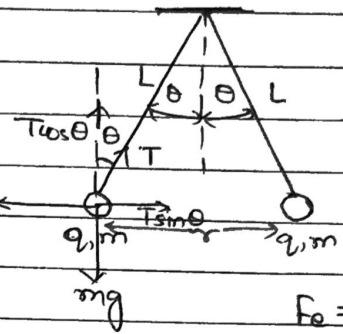
$$\tan \theta = \frac{kq^2}{r^2 mg}$$

$$\Rightarrow q^2 = \frac{mg r^2 \tan \theta}{k}$$

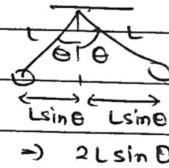
$$q^2 = 4\pi\epsilon_0 \cdot mg (2L \sin \theta)^2 \tan \theta$$

$$q^2 = 4\pi\epsilon_0 \cdot 4L^2 \sin^2 \theta \tan \theta$$

$$q = \sqrt{16\pi\epsilon_0 mg L^2 \sin^2 \theta \tan \theta}$$



$$F_e = \frac{kq^2}{r^2}$$



- Q- Two small spherical balls each carrying a charge $q = 10 \mu\text{C}$ are suspended by two insulating threads of equal lengths 1 m each, from a point fixed in the ceiling. It is found that in equilibrium threads are separated by an angle 60° b/w them, as shown in the fig. What is the Tension in the threads :- (Given, $\frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ Nm/C}^2$)

(a) 18 N

(b) 1.8 N

(c) 0.18 N

(d) None of these

key point :



If θ is very small,

$$\tan \theta \approx \sin \theta \approx \theta$$

$$x^3 = \frac{kq^2(2y)}{mg} = \frac{kq^2(2l)}{mg}$$

$$\Rightarrow x^3 \propto q^2$$

Page No.
 Date

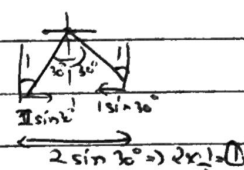
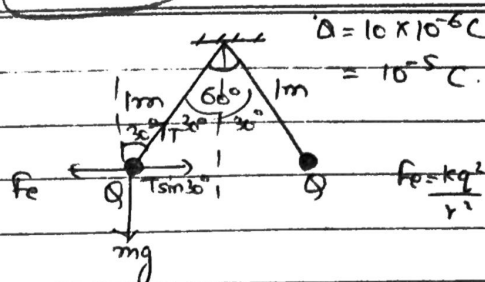
$$T \sin 30^\circ = F_e$$

$$T \times \frac{1}{2} = \frac{kq^2}{r^2}$$

$$T \times \frac{1}{2} = \frac{9 \times 10^9 \times (10^{-5})^2}{(1)^2}$$

$$T = 18 \times 10^{-1}$$

$$T = 1.8 \text{ N}$$



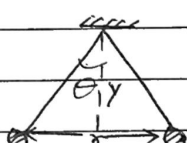
Q- Two pith balls carrying equal charges are suspended from a common point by strings of equal length, the equilibrium separation b/w them is r . Now the strings are rigidly clamped at half the height. The equilibrium separation b/w the balls now become (2013)

a) $\left(\frac{1}{\sqrt{2}}\right)^2$

b) $\frac{r}{\sqrt{2}}$

c) $\left(\frac{2r}{\sqrt{3}}\right)$

d) $\left(\frac{2r}{3}\right)$



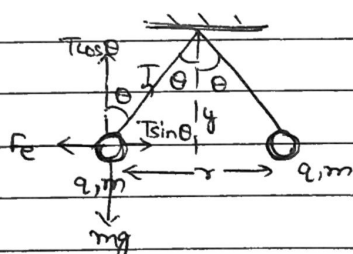
key point

$$x^3 \propto y$$

$$x^3 \propto y$$

$$\left(\frac{r}{2}\right)^3 \propto \frac{r}{2}$$

$$\left(\frac{r}{2}\right)^3 = \frac{r}{2}$$



$$T \sin \theta = F_e$$

$$T \cos \theta = mg$$

$$\therefore \tan \theta = \frac{F_e}{mg}$$

Case I : $\tan \theta = \frac{F_e}{mg}$

$$\frac{r}{2y} = \frac{kq^2}{r^2 mg} \quad \text{--- (1)}$$

Case II : $\tan \theta' = \frac{F_e}{mg}$

$$\frac{r'}{2y} = \frac{kq^2}{r'^2 mg} \quad \text{--- (2)}$$

$$\Rightarrow \text{from (1) \& (2) } (3) \div (1)$$

$$\frac{r'}{2y} = \frac{2r'}{2y}$$

$$\frac{r'}{y} = \frac{kq^2}{r'^2 mg}$$

$$\frac{r}{2y} = \frac{kq^2}{r'^2 mg}$$

$$\frac{2r'}{r} = \frac{r^2}{r'^2}$$

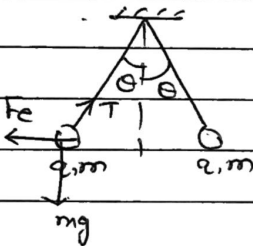
$$2r'^3 = r^3$$

$$r'^3 = \frac{r^3}{2}$$

$$r' = \frac{r}{(2)^{1/3}} = \frac{r}{\sqrt[3]{2}}$$

Summary

Learn this



$$\tan \theta = \frac{F_e}{mg}$$

$$T = \sqrt{F_e^2 + mg^2}$$

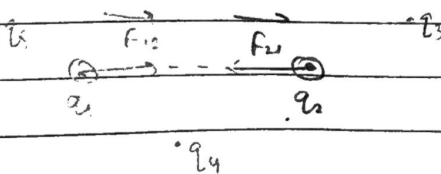
Principle of Superposition

- If there are 3 or more charges, then net force on any one charge is vector sum of all forces on it due to remaining charges.

q_1 q_2

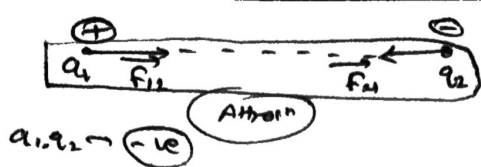
 $F_{net} = \vec{F}_1 + \vec{F}_2$

Note: The force between any two charges is unaffected by the presence of third charge.



Conclusion:

- F_{12} & F_{21} will remain constant
- Net force on q_1 & q_2 may be 0 or not.



a) $q_1 q_2 < 0$

b) $q_1 q_2 > 0$

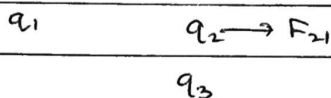
c) $q_1 q_2 = 0$

d) Date / month / year

Page No. _____
Date _____

$q_1 \quad q_2 \quad q_3 \quad q_4 \quad q_5 \quad q_6 \dots q_n$
net force on
 n^{th} charge $= \vec{F}_n = \vec{F}_{n1} + \vec{F}_{n2} + \vec{F}_{n3} + \dots$

- Q. A charge q_1 exerts some force on a second charge q_2 .
If a third charge q_3 is brought near q_2 , then the force exerted by q_1 on q_2
- decreases
 - increases
 - remains the same
 - increases, if q_3 is of same sign as q_1 and decreases, if q_3 is of opp. sign as q_1 .



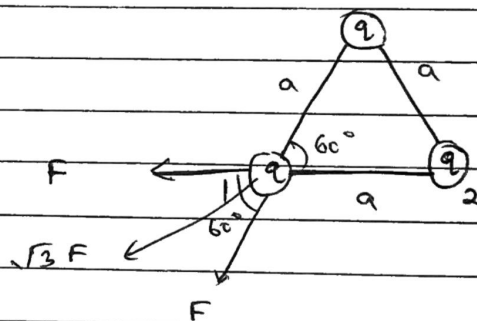
- Q. Three equal charges (q) are placed at the corners of an equilateral triangle. The force on any charge is:

a) $\frac{3kq^2}{a^2}$

~~b) $\frac{\sqrt{3}kq^2}{a^2}$~~

c) $\frac{\sqrt{3}kq^2}{a^3}$

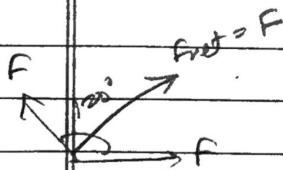
d) $\frac{\sqrt{3}kq^2}{a^2}$



$\therefore$ Net force on 1:

$= \sqrt{3}F$

$= \frac{\sqrt{3}kq^2}{a^2}$



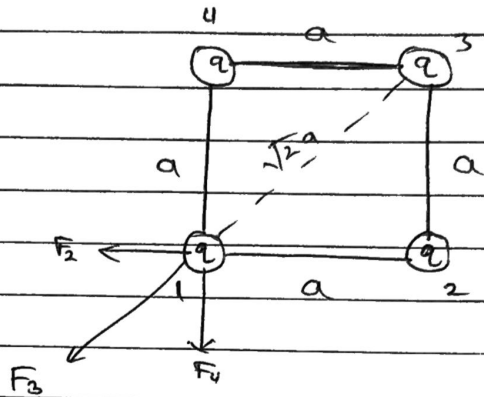
- Q. Four equal point charges each ' q ' are placed on the four corners of a square of side ' a '. Calculate the force on any one of the charges.

a) $\frac{kq^2 (2 + \sqrt{2})}{a^2}$

b) $\frac{kq^2 (2 + \frac{1}{\sqrt{2}})}{a^2}$

~~c)~~ $\frac{kq^2 (\sqrt{2} + \frac{1}{2})}{a^2}$

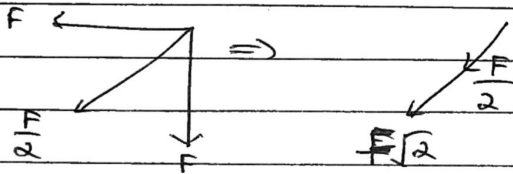
d) None of these



$$F_2 = \frac{kq^2}{a^2} = F$$

$$F_4 = \frac{kq^2}{a^2} = F$$

$$F_3 = \frac{kq^2}{(\sqrt{2}a)^2} = \frac{kq^2}{2a^2} = \frac{F}{2}$$



$$\therefore \text{Net force} = \frac{F}{2} + F\sqrt{2}$$

$$= \frac{kq^2}{a^2} \left(\frac{1}{2} + \sqrt{2} \right)$$

Attraction can be b/w the 4 neutral charge but repulsion only b/w same charges.
 r) cgs unit : $1C = 3 \times 10^9 \text{ stat. C}$
 $1C = 3 \times 10^9 \text{ esu}$ & $1C = \frac{1}{10} \text{ emu}$
 $K = 1$ (for air/vacuum) $\rightarrow K = \infty$ (for metals)

2) $\frac{F_{air}}{F_{med}} = K = \epsilon_r$ $\frac{F_o}{F_m} = \frac{\epsilon_m}{\epsilon_o} = \epsilon_r \text{ or } K \Rightarrow \epsilon_m = \epsilon_r \cdot \epsilon_o$ $1 \leq K \leq \infty$

3) Condition for the force to be identical b/w two point charges separated by two diff. mediums.

$K_1 r_1^2 = K_2 r_2^2$
 If 1st medium is air $\Rightarrow (K_1 = 1)$

$r_{air} = \sqrt{K_{med}} \cdot r_{med}$

$F = \frac{k q_1 q_2}{(r - t + \sqrt{K} t)^2}$

$E_{air} = \frac{\rho r}{4\pi\epsilon_o(r^2 + a^2)^{3/2}}$
 $E_{med} = \frac{\rho}{4\pi\epsilon_o(\sqrt{K}r^2 + a^2)^{3/2}}$

4) Electric field intensity at line joining two charges :-

$E = \left[\frac{\sqrt{\text{smaller charge}}}{\sqrt{\text{Bigger charge}} - \sqrt{\text{smaller charge}}} \right] a$

5) Electric field intensity due to distributed charge =

$E = \frac{\lambda K \lambda}{r} = \frac{\lambda}{2\pi\epsilon_o r}$

6) Electric field intensity due to an arc of charge at its centre.

$E_{centre} = \int dE = \frac{\lambda K \lambda}{R} \frac{\sin \theta}{2}$

for semicircular arc, $\theta = \pi$

$E_{centre} = \frac{\lambda K \lambda}{R}$

7) Electric field intensity due to a ring of charge at a distance 'n' from the centre on the axis of the Ring.

$E_{axis} = \frac{k Q n}{(R^2 + n^2)^{3/2}}$

$\frac{dE}{dn} = 0$

$n = \frac{R}{\sqrt{2}}$ E_{max}

ii) Time period of SHM of a charge q released very close to the centre of the ring.

$T = 2\pi \sqrt{\frac{4\pi\epsilon_o m R^3}{Qq}}$

8) Effect of Simple pendulum placed in External Magnetic field.

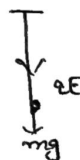
$T = 2\pi \sqrt{\frac{l}{g_{eff}}}$

Case I: Pendulum oscillates vertically downward

$mg_{eff} = mg + qE$

$g_{eff} = g + \frac{qE}{m}$

$T = 2\pi \sqrt{\frac{l}{g + \frac{qE}{m}}}$



Case II: Pendulum rotates in vertical upward.

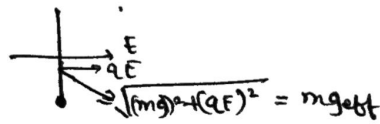
$mg_{eff} = mg - qE$

$g_{eff} = g - \frac{qE}{m}$

$T = 2\pi \sqrt{\frac{l}{g - \frac{qE}{m}}}$



Case III: If Pendulum is placed in a horizontal electric field.



$g_{eff} = \sqrt{g^2 + \left(\frac{qE}{m}\right)^2}$

$T = 2\pi \sqrt{\frac{l}{\sqrt{g^2 + \left(\frac{qE}{m}\right)^2}}}$

$$q) \lambda = \sqrt{\frac{PE}{I}}$$

$$T = \frac{1}{\omega} \sqrt{\frac{I}{PE}}$$

10) Integral form of Relation b/w Potential diff. & Electric field.

$$V_A - V_B = \int_{x_A}^{x_B} E_x dx + \int_{y_A}^{y_B} E_y dy + \int_{z_A}^{z_B} E_z dz$$

If potential is given, & Electric field is to be calculated:-

$$\vec{E} = - \left(\frac{\partial V}{\partial x} \hat{i} + \frac{\partial V}{\partial y} \hat{j} + \frac{\partial V}{\partial z} \hat{k} \right)$$

$$\vec{E} = -\nabla V$$

How many cubes needed to cover charge

i) Gauss



$$\phi = \frac{q}{\epsilon_0}$$

ii)



$$\phi = \frac{q}{8\epsilon_0}$$

iii)



$$\phi = \frac{q}{4\epsilon_0}$$

⇒ A charge Q is placed at corner of cube of length L . The electric flux link to one of the face not touching the charge Q is $\frac{Q}{24\epsilon_0}$

12) Electric field & Potential diff. due to infinitely long charge,

$$E = \frac{\lambda}{2\pi\epsilon_0 r} = \frac{2K\lambda}{r}$$

$$V_A - V_B = 2K\lambda \ln \frac{b}{a}$$

11) electric field & potential diff. due to a sheet of charge

$$E = \frac{\sigma}{2\epsilon_0}$$

$$V_A - V_B = \frac{\sigma}{\epsilon_0} (b-a)$$

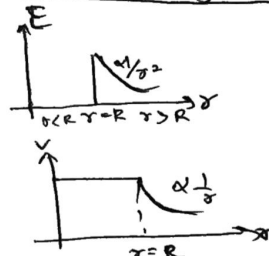
E due to conducting sheet = $\frac{\sigma}{\epsilon_0}$
non-conducting sheet = $\frac{\sigma}{2\epsilon_0}$

11) Electric field & potential at all points due to

hollow conducting, hollow non-conducting solid conducting

Electric field
Potential

Outside ($r > R$)	Surface ($r = R$)	Inside ($r < R$)
$E_{out} \propto \frac{KQ}{r^2}$	$E_{surf.} = \frac{KQ}{R^2}$	$E_{in} = 0$
$V_{out} \propto \frac{KQ}{r}$	$V_{surf.} = \frac{KQ}{R}$	$V_{in} = V_{surface}$

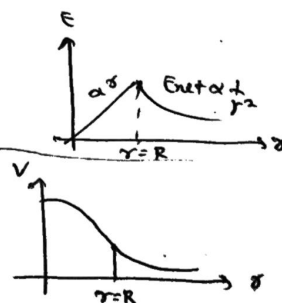


iv) Electric field & potential at all points due to

solid non-conducting sphere

Potential

Outside ($r > R$)	Surface ($r = R$)	Inside ($r < R$)
$E_{out} = \frac{kQ}{r^2}$	$E = \frac{kQ}{R^2}$	$E_{in} = \frac{kQr}{R^3}$ or $E = \frac{\rho r}{3\epsilon_0}$
$V_{out} = \frac{KQ}{r}$	$V_{surf.} = \frac{KQ}{R}$	$V_{centre} = \frac{3kQ}{2R}$ $V_{centre} = \frac{3}{2} V_{surface}$



13) Electric field at random position

$$E_{net} = \frac{k\rho}{r^3} \int 1 + 3\cos^2\theta$$

$$\alpha = \tan^{-1} \left[\frac{\tan\theta}{2} \right]$$

14) ⊥ dist. of charge q in uniform E after travelling distance x is

$$y = \frac{qEx^2}{2mv^2}$$