

Chapter Name : Trigonometry

- 1) Given that $\tan \theta = \frac{5}{12}$ and θ is an acute angle, find $\sin \theta$ and $\cos \theta$.
- 2) If $5 \sin \theta = 3$, find the value of $\frac{\sec \theta - \tan \theta}{\sec \theta + \tan \theta}$.
- 3) If θ is an acute angle and $\sin \theta = \cos \theta$, find the value of $2 \tan^2 \theta + \sin^2 \theta - 1$.
- 4) Prove the following: $\frac{\cos \theta}{\sin(90^\circ - \theta)} + \frac{\sin \theta}{\cos(90^\circ - \theta)} = 2$.
- 5) Prove that $\cos^2 30^\circ + \sin 30^\circ + \tan^2 45^\circ = \frac{9}{4}$.
- 6) Without using trigonometrical tables, evaluate : $\sin^2 34^\circ + \sin^2 56^\circ + 2 \tan 18^\circ \tan 72^\circ - \cot^2 30^\circ$.
- 7) Prove that $\frac{\cos(90-\theta) \sec(90-\theta) \tan \theta}{\operatorname{cosec}(90-\theta) \sin(90-\theta) \cot(90-\theta)} + \frac{\tan(90-\theta)}{\cot \theta} = 2$.
- 8) If $\sin \theta = \frac{p}{q}$, find the value of $\sec \theta + \tan \theta$
- 9) If $a \cos A = 1$, $b \cot A = 1$, prove that $a^2 - b^2 = 1$
- 10) Prove that: $\frac{\tan 60^\circ - \tan 30^\circ}{1 + \tan 60^\circ \tan 30^\circ} = \tan 30^\circ$
- 11) $\cos A = \frac{5}{13}$. Find the value of $(\sin A - \cot A) / 2 \tan A$
- 12) Evaluate: $\frac{\cos 75^\circ}{\sin 15^\circ} + \frac{\sin 12^\circ}{\cos 78^\circ} - \frac{\cos 18^\circ}{\sin 72^\circ}$.
- 13) If 3θ is an acute angle, solve the following equation for : $2 \sin 3\theta = \sqrt{3}$.
- 14) If $\tan \theta = \frac{5}{12}$, find the value of $\frac{\cos \theta + \sin \theta}{\cos \theta - \sin \theta}$.
- 15) Find the value of : $\frac{\sec 29^\circ}{\operatorname{cosec} 61^\circ} + 2 \cot 8^\circ \cot 17^\circ \cot 45^\circ \cot 73^\circ \cot 82^\circ - 3(\sin^2 38^\circ + \sin^2 52^\circ)$
- 16) Simplify the following : $\frac{\operatorname{cosec}(90^\circ - \theta) \sin(90^\circ - \theta) \cot(90^\circ - \theta)}{\cos(90^\circ - \theta) \sec(90^\circ - \theta) \tan \theta} + \frac{\cot \theta}{\tan(90^\circ - \theta)}$.
- 17) If $\sin \theta + \operatorname{cosec} \theta = 2$, find the value of $\sin^2 \theta + \operatorname{cosec}^2 \theta$.
- 18) If $\sin \theta + \operatorname{cosec} \theta = 2$, find the value of $\sin^5 \theta + \operatorname{cosec}^5 \theta$.
- 19) Taking $A = 30^\circ$ verify that $\cos^4 A - \sin^4 A = \cos 2A$
- 20) If $\sin A = \frac{1}{3}$, evaluate $\cos A \operatorname{cosec} A + \tan A \sec A$.
- 21) Find the value of x if $\cos x = \cos 60^\circ \cos 30^\circ + \sin 60^\circ \sin 30^\circ$.
- 22) If $A + B = 90^\circ$, prove that $\sqrt{\frac{\tan A \tan B + \tan A \cot B}{\sin A \sec B} - \frac{\sin^2 B}{\cos^2 A}} = \tan A$.
- 23) In the adjoining figure, AM is perpendicular to BC.
If $\tan B = \frac{3}{4}$, $\tan C = \frac{5}{12}$ and $BC = 56$ cm, calculate the length of AM.
- 24) Given $4 \sin A = 3 \cos A$, find the value of : (i) $\sin A$ (ii) $\cot^2 A - \operatorname{cosec}^2 A$.

