QUADRILATERAL TEST -1

- 1. ABCD is a rhombus. Show that diagonal AC bisects $\angle A$ as well as $\angle C$ and diagonal BD bisects $\angle B$ as well as $\angle D$.
- 2. The angles A, B,C,D of a quadrilateral are in the ratio of 2:4:5:7.Find the measure of these angles. What type of quadrilateral is it? Give reasons
- 3. ABCD is a quadrilateral in which P, Q,R, S are the midpoints of the sides AB, BC, CD, and DA respectively. Show that PQRS is a parallelogram
- 4. In parallelogram ABCD, two points P and Q are taken on diagonal BD such that DP = BQ (see figure). Show that

(i) $\triangle APD \cong \triangle CQB$ (ii) AP = CQ(iii) $\triangle AQB \cong \triangle CPD$ (iv) AQ = CP(v) APCQ is a parallelogram.

- 5. In \triangle ABC and \triangle DEF, AB = DE, AB || DE, BC = EF and BC || EF. Vertices A, B and C are joined to vertices D, E and F, respectively (see figure). Show that
 - i. quadrilateral ABED is a parallelogram
 - ii. quadrilateral BEFC is a parallelogram
 - iii. AD || CF and AD = CF
 - iv. quadrilateral ACFD is a parallelogram
 - v. AC = DF
 - vi. $\Delta ABC \cong \Delta DEF$
- 6. ABCD is a trapezium in which AB || CD and AD = BC (see figure). Show that
 - i. ∠A=∠B
 - ii. ∠C=∠D
 - iii. $\triangle ABC \cong \triangle BAD$
 - iv. diagonal AC = diagonal BD



- 7. I, m and n are three parallel lines intersected by transversals p and q such that I, m and n cut off equal intercepts AB and BC on p (see fig. 8.28). Show that I, m and n cut off equal intercepts DE and EF on q also.
- 8. ABCD is a parallelogram in which P and Q are mid-points of opposite sides AB and CD (see fig.)If AQ intersects DP at S and BQ intersects CP at R, show that:
 - i. APCQ is a parallelogram.
 - ii. DPBQ is a parallelogram.
 - iii. PSQR is a parallelogram.



9. Two parallel lines I and m are intersected by a transversal p (see fig). Show that the quadrilateral formed by the bisectors of interior angles is a rectangle.



10. Prove that the diagonals of a square are equal and perpendicular to each other.