

# Hexagon

In geometry, a **hexagon** (from Greek ἕξ, *hex*, meaning "six", and γωνία, *gonía*, meaning "corner, angle") is a six-sided polygon.<sup>[1]</sup> The total of the internal angles of any simple (non-self-intersecting) hexagon is 720°.

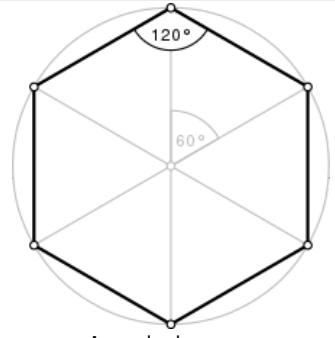

## Regular hexagon

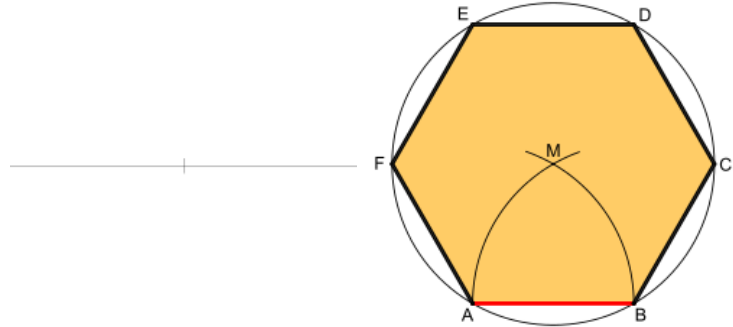
A *regular hexagon* has *Schläfli symbol* {6}<sup>[2]</sup> and can also be constructed as a *truncated equilateral triangle*, t{3}, which alternates two types of edges.

A regular hexagon is defined as a hexagon that is both *equilateral* and *equiangular*. It is *bicentric*, meaning that it is both *cyclic* (has a circumscribed circle) and *tangential* (has an inscribed circle).

The common length of the sides equals the radius of the *circumscribed circle* or *circumcircle*, which equals  $\frac{2}{\sqrt{3}}$  times the *apothem* (radius of the *inscribed circle*). All internal angles are 120 degrees. A regular hexagon has six *rotational symmetries* (*rotational symmetry of order six*) and six *reflection symmetries* (*six lines of symmetry*), making up the *dihedral group* D<sub>6</sub>. The longest diagonals of a regular hexagon, connecting diametrically opposite vertices, are twice the length of one side. From this it can be seen that a *triangle* with a vertex at the center of the regular hexagon and sharing one side with the hexagon is *equilateral*, and that the regular hexagon can be partitioned into six equilateral triangles.

Like *squares* and *equilateral triangles*, regular hexagons fit together without any gaps to *tile the plane* (three hexagons meeting at every vertex), and so are useful for constructing *tessellations*. The cells of a *beehive honeycomb* are hexagonal for this reason and because the shape makes efficient use of space and building materials. The *Voronoi diagram* of a regular triangular lattice is the honeycomb tessellation of hexagons. It is not usually considered a *triambus*, although it is equilateral.

Regular hexagon	
	
A regular hexagon	
<b>Type</b>	Regular polygon
<b>Edges and vertices</b>	6
<b>Schläfli symbol</b>	{6}, t{3}
<b>Coxeter–Dynkin diagrams</b>	
<b>Symmetry group</b>	Dihedral (D <sub>6</sub> ), order 2×6
<b>Internal angle (degrees)</b>	120°
<b>Properties</b>	Convex, cyclic, equilateral, isogonal, isotoxal
<b>Dual polygon</b>	Self



A step-by-step animation of the construction of a regular hexagon using *compass and straightedge*, given by *Euclid's Elements*, Book IV, Proposition 15: this is possible as  $6 = 2 \times 3$ , a product of a power of two and distinct Fermat primes.

When the side length  $\overline{AB}$  is given, drawing a circular arc from point A and point B gives the *intersection M*, the center of the *circumscribed circle*. Transfer the *line segment AB* four times on the circumscribed circle and connect the corner points.

## Parameters

The maximal *diameter* (which corresponds to the long *diagonal* of the hexagon), *D*, is twice the maximal radius or *circumradius*, *R*, which equals the side length, *t*. The minimal diameter or the diameter of the *inscribed circle* (separation of parallel sides, flat-to-flat distance, short diagonal or height when resting on a flat base), *d*, is twice the minimal radius or *inradius*, *r*. The maxima and minima are related by the same factor:

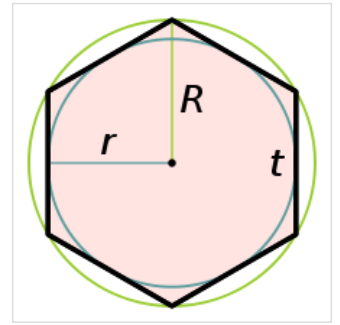
$$\frac{1}{2}d = r = \cos(30^\circ)R = \frac{\sqrt{3}}{2}R = \frac{\sqrt{3}}{2}t \quad \text{and, similarly, } d = \frac{\sqrt{3}}{2}D.$$

The area of a regular hexagon

$$\begin{aligned}
A &= \frac{3\sqrt{3}}{2} R^2 = 3Rr = 2\sqrt{3}r^2 \\
&= \frac{3\sqrt{3}}{8} D^2 = \frac{3}{4} Dd = \frac{\sqrt{3}}{2} d^2 \\
&\approx 2.598R^2 \approx 3.464r^2 \\
&\approx 0.6495D^2 \approx 0.866d^2.
\end{aligned}$$

For any regular polygon, the area can also be expressed in terms of the apothem  $a$  and the perimeter  $p$ . For the regular hexagon these are given by  $a = r$ , and  $p = 6R = 4r\sqrt{3}$ , so

$$\begin{aligned}
A &= \frac{ap}{2} \\
&= \frac{r \cdot 4r\sqrt{3}}{2} = 2r^2\sqrt{3} \\
&\approx 3.464r^2.
\end{aligned}$$



$R =$  Circumradius;  $r =$  Inradius;  $t =$  side length

The regular hexagon fills the fraction  $\frac{3\sqrt{3}}{2\pi} \approx 0.8270$  of its circumscribed circle.

If a regular hexagon has successive vertices A, B, C, D, E, F and if P is any point on the circumcircle between B and C, then  $PE + PF = PA + PB + PC + PD$ .

It follows from the ratio of circumradius to inradius that the height-to-width ratio of a regular hexagon is 1:1.1547005; that is, a hexagon with a long diagonal of 1.0000000 will have a distance of 0.8660254 between parallel sides.

## Point in plane

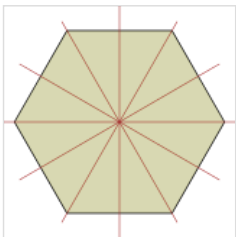
For an arbitrary point in the plane of a regular hexagon with circumradius  $R$ , whose distances to the centroid of the regular hexagon and its six vertices are  $L$  and  $d_i$  respectively, we have<sup>[3]</sup>

$$\begin{aligned}
d_1^2 + d_4^2 &= d_2^2 + d_5^2 = d_3^2 + d_6^2 = 2(R^2 + L^2), \\
d_1^2 + d_3^2 + d_5^2 &= d_2^2 + d_4^2 + d_6^2 = 3(R^2 + L^2), \\
d_1^4 + d_3^4 + d_5^4 &= d_2^4 + d_4^4 + d_6^4 = 3((R^2 + L^2)^2 + 2R^2L^2).
\end{aligned}$$

If  $d_i$  are the distances from the vertices of a regular hexagon to any point on its circumcircle, then<sup>[3]</sup>

$$\left(\sum_{i=1}^6 d_i^2\right)^2 = 4 \sum_{i=1}^6 d_i^4.$$

## Symmetry



The six lines of reflection of a regular hexagon, with  $D_{6h}$  or **r12** symmetry, order 12.

The *regular hexagon* has  $D_6$  symmetry. There are 16 subgroups. There are 8 up to isomorphism: itself ( $D_6$ ), 2 dihedral: ( $D_3, D_2$ ), 4 cyclic: ( $Z_6, Z_3, Z_2, Z_1$ ) and the trivial (e)

These symmetries express nine distinct symmetries of a regular hexagon. John Conway labels these by a letter and group order.<sup>[4]</sup> **r12** is full symmetry, and **a1** is no symmetry. **p6**, an isogonal hexagon constructed by three mirrors can alternate long and short edges, and **d6**, an isotoxal hexagon constructed

with equal edge lengths, but vertices alternating two different internal angles. These two forms are duals of each other and have half the symmetry order of the regular hexagon. The **i4** forms are regular hexagons flattened or stretched along one symmetry direction. It can be seen as an elongated rhombus, while **d2** and **p2** can be seen as horizontally and vertically elongated kites. **g2** hexagons, with opposite sides parallel are also called hexagonal parallelogons.

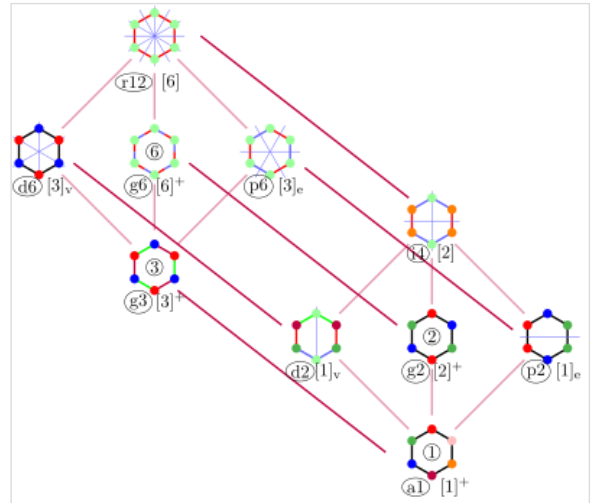
Each subgroup symmetry allows one or more degrees of freedom for irregular forms. Only the **g6** subgroup has no degrees of freedom but can be seen as directed edges.

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Hexagons of symmetry **g2**, **i4**, and **r12**, as parallelogons can tessellate the Euclidean plane by translation. Other hexagon shapes can tile the plane with different orientations.

### Example hexagons by symmetry

	<b>r12</b> regular			<b>i4</b>	
<b>d6</b> isotoxal	<b>g6</b> directed	<b>p6</b> isogonal	<b>d2</b>	<b>g2</b> general parallelogon	<b>p2</b>
	<b>g3</b>			<b>a1</b>	



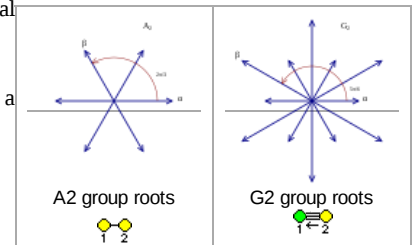
The dihedral symmetries are divided depending on whether they pass through vertices (**d** for diagonal) or edges (**p** for perpendiculars). Cyclic symmetries in the middle column are labeled as **g** for their central gyration orders. Full symmetry of the regular form is **r12** and no symmetry is labeled **a1**.

$p6m$ (*632)	$cmm$ (2*22)	$p2$ (2222)	$p31m$ (3*3)	$pmg$ (22*)	$pg$ (xx)
<b>r12</b>	<b>i4</b>	<b>g2</b>	<b>d2</b>	<b>d2</b>	<b>a1</b>
<b>Dih<sub>6</sub></b>	<b>Dih<sub>2</sub></b>	<b>Z<sub>2</sub></b>		<b>Dih<sub>1</sub></b>	<b>Z<sub>1</sub></b>

## A2 and G2 groups

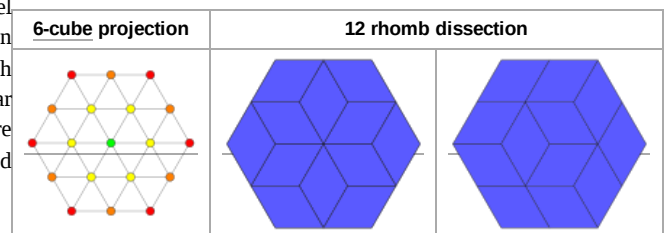
The 6 roots of the simple Lie group  $A_2$ , represented by a Dynkin diagram , are in a regular hexagonal pattern. The two simple roots have a  $120^\circ$  angle between them.

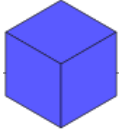
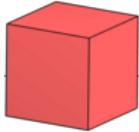
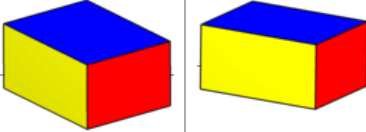
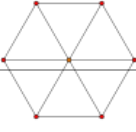
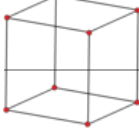
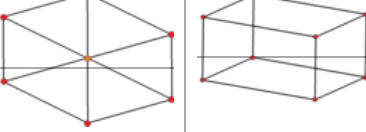
The 12 roots of the Exceptional Lie group  $G_2$ , represented by a Dynkin diagram , are also in a hexagonal pattern. The two simple roots of two lengths have a  $150^\circ$  angle between them.



## Dissection

Coxeter states that every zonogon (a  $2m$ -gon whose opposite sides are parallel and of equal length) can be dissected into  $\frac{1}{2}m(m - 1)$  parallelograms.<sup>[5]</sup> In particular this is true for regular polygons with evenly many sides, in which case the parallelograms are all rhombi. This decomposition of a regular hexagon is based on a Petrie polygon projection of a cube, with 3 of 6 square faces. Other parallelogons and projective directions of the cube are dissected within rectangular cuboids.



Dissection of hexagons into three rhombs and parallelograms			
	Rhombus	Parallelograms	
2D			
	Regular {6}	Hexagonal parallelograms	
	Square faces	Rectangular faces	
3D			
	Cube	Rectangular cuboid	


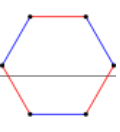
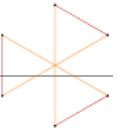
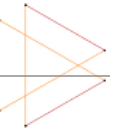
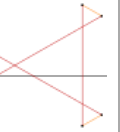

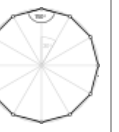
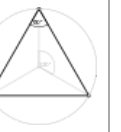
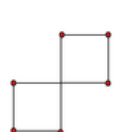


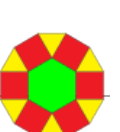
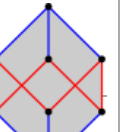

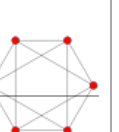
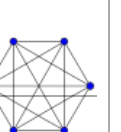
## Related polygons and tilings

A regular hexagon has Schläfli symbol {6}. A regular hexagon is a part of the regular hexagonal tiling, {6,3}, with three hexagonal faces around each vertex.

A regular hexagon can also be created as a truncated equilateral triangle, with Schläfli symbol  $t\{3\}$ . Seen with two types (colors) of edges, this form only has  $D_3$  symmetry.

A truncated hexagon,  $t\{6\}$ , is a dodecagon, {12}, alternating two types (colors) of edges. An alternated hexagon,  $h\{6\}$ , is an equilateral triangle, {3}. A regular hexagon can be stellated with equilateral triangles on its edges, creating a hexagram. A regular hexagon can be dissected into six equilateral triangles by adding a center point. This pattern repeats within the regular triangular tiling.

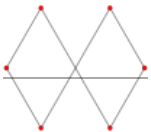
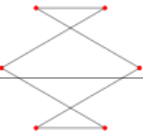
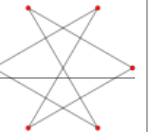
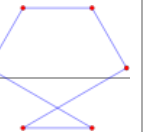
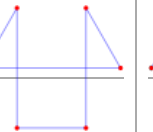
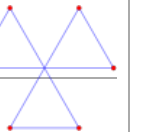
A regular hexagon can be extended into a regular dodecagon by adding alternating squares and equilateral triangles around it. This pattern repeats within the rhombitrihexagonal tiling.

							
Regular {6}	Truncated $t\{3\} = \{6\}$	Hypertruncated triangles	Stellated Star figure $2\{3\}$	Truncated $t\{6\} = \{12\}$	Alternated $h\{6\} = \{3\}$		
							
Crossed hexagon	A concave hexagon	A self-intersecting hexagon (star polygon)	Extended Central {6} in {12}	A skew hexagon, within cube	Dissected {6}	projection octahedron	Complete graph

## Self-crossing hexagons

There are six self-crossing hexagons with the vertex arrangement of the regular hexagon:

Self-intersecting hexagons with regular vertices

$Dih_2$		$Dih_1$		$Dih_3$
				
Figure-eight	Center-flip	Unicursal	Fish-tail	Double-tail
				
				Triple-tail

## Hexagonal structures

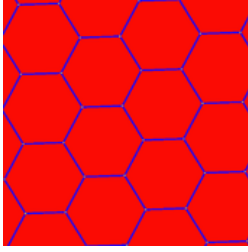
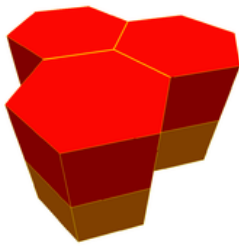
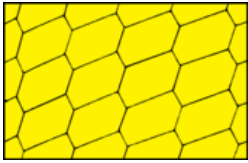
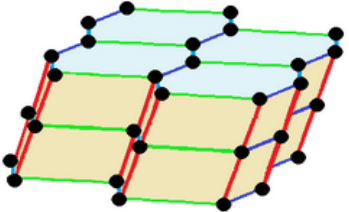
From bees' honeycombs to the Giant's Causeway, hexagonal patterns are prevalent in nature due to their efficiency. In a hexagonal grid each line is as short as it can possibly be if a large area is to be filled with the fewest hexagons. This means that honeycombs require less wax to construct and gain much strength under compression.



Giant's Causeway closeup

Irregular hexagons with parallel opposite edges are called parallelogons and can also tile the plane by translation. In three dimensions, hexagonal prisms with parallel opposite faces are called parallelohedrons and these can tessellate 3-space by translation.

Hexagonal prism tessellations

Form	Hexagonal tiling	Hexagonal prismatic honeycomb
Regular		
Parallelogonal		

## Tessellations by hexagons

In addition to the regular hexagon, which determines a unique tessellation of the plane, any irregular hexagon which satisfies the Conway criterion will tile the plane.

## Hexagon inscribed in a conic section

Pascal's theorem (also known as the "Hexagrammum Mysticum Theorem") states that if an arbitrary hexagon is inscribed in any conic section, and pairs of opposite sides are extended until they meet, the three intersection points will lie on a straight line, the "Pascal line" of that configuration.

## Cyclic hexagon

The Lemoine hexagon is a cyclic hexagon (one inscribed in a circle) with vertices given by the six intersections of the edges of a triangle and the three lines that are parallel to the edges that pass through its symmedian point.

If the successive sides of a cyclic hexagon are  $a, b, c, d, e, f$ , then the three main diagonals intersect in a single point if and only if  $ace = bdf$ .<sup>[6]</sup>

If, for each side of a cyclic hexagon, the adjacent sides are extended to their intersection, forming a triangle exterior to the given side, then the segments connecting the circumcenters of opposite triangles are concurrent.<sup>[7]</sup>

If a hexagon has vertices on the circumcircle of an acute triangle at the six points (including three triangle vertices) where the extended altitudes of the triangle meet the circumcircle, then the area of the hexagon is twice the area of the triangle.<sup>[8]: p. 179</sup>

## Hexagon tangential to a conic section

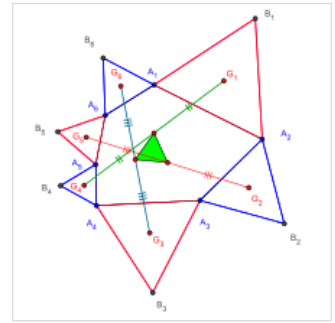
Let ABCDEF be a hexagon formed by six tangent lines of a conic section. Then Brianchon's theorem states that the three main diagonals AD, BE, and CF intersect at a single point.

In a hexagon that is tangential to a circle and that has consecutive sides  $a, b, c, d, e$ , and  $f$ .<sup>[9]</sup>

$$a + c + e = b + d + f.$$

## Equilateral triangles on the sides of an arbitrary hexagon

If an equilateral triangle is constructed externally on each side of any hexagon, then the midpoints of the segments connecting the centroids of opposite triangles form another equilateral triangle.<sup>[10]: Thm. 1</sup>



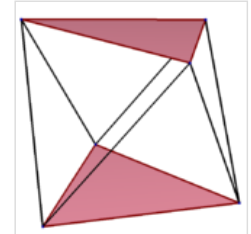
Equilateral triangles on the sides of an arbitrary hexagon

## Skew hexagon

A **skew hexagon** is a skew polygon with six vertices and edges but not existing on the same plane. The interior of such a hexagon is not generally defined. A *skew zig-zag hexagon* has vertices alternating between two parallel planes.

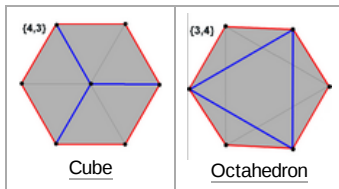
A **regular skew hexagon** is vertex-transitive with equal edge lengths. In three dimensions it will be a zig-zag skew hexagon and can be seen in the vertices and side edges of a triangular antiprism with the same  $D_{3d}$ ,  $[2^+,6]$  symmetry, order 12.

The cube and octahedron (same as triangular antiprism) have regular skew hexagons as petrie polygons.



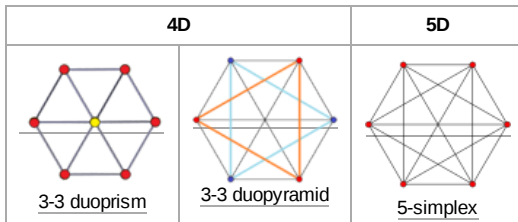
A regular skew hexagon seen as edges (black) of a triangular antiprism, symmetry  $D_{3d}$ ,  $[2^+,6]$ ,  $(2^*3)$ , order 12.

Skew hexagons on 3-fold axes



## Petrie polygons

The regular skew hexagon is the Petrie polygon for these higher dimensional regular, uniform and dual polyhedra and polytopes, shown in these skew orthogonal projections:



## Convex equilateral hexagon

A *principal diagonal* of a hexagon is a diagonal which divides the hexagon into quadrilaterals. In any convex equilateral hexagon (one with all sides equal) with common side  $a$ , there exists<sup>[11]:p.184,#286.3</sup> a principal diagonal  $d_1$  such that

$$\frac{d_1}{a} \leq 2$$

and a principal diagonal  $d_2$  such that

$$\frac{d_2}{a} > \sqrt{3}.$$

## Polyhedra with hexagons

There is no Platonic solid made of only regular hexagons, because the hexagons tessellate, not allowing the result to "fold up". The Archimedean solids with some hexagonal faces are the truncated tetrahedron, truncated octahedron, truncated icosahedron (of soccer ball and fullerene fame), truncated cuboctahedron and the truncated icosidodecahedron. These hexagons can be considered truncated triangles, with Coxeter diagrams of the form  $\odot - \odot_p - \odot$  and  $\odot - \odot_p - \odot$ .

Hexagons in Archimedean solids				
Tetrahedral	Octahedral		Icosahedral	
truncated tetrahedron	truncated octahedron	truncated cuboctahedron	truncated icosahedron	truncated icosidodecahedron





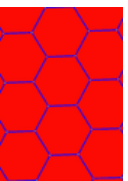
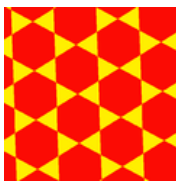
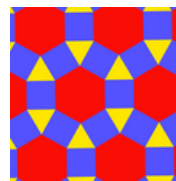
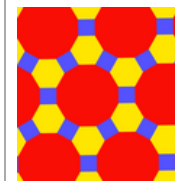
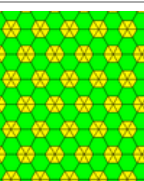
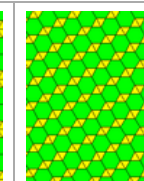
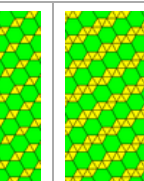
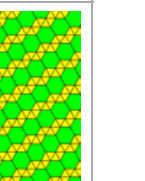
There are other symmetry polyhedra with stretched or flattened hexagons, like these Goldberg polyhedron G(2,0):

Hexagons in Goldberg polyhedra		
Tetrahedral	Octahedral	Icosahedral
Chamfered tetrahedron	Chamfered cube	Chamfered dodecahedron

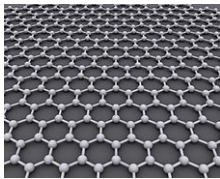
There are also 9 Johnson solids with regular hexagons:

Johnson solids with hexagons		
triangular cupola	elongated triangular cupola	gyroelongated triangular cupola
augmented hexagonal prism	parabiaugmented hexagonal prism	metabiaugmented hexagonal prism
triauxmented hexagonal prism	augmented truncated tetrahedron	triangular hebesphenorotunda

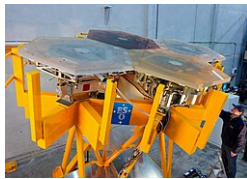
Prismoids with hexagons		
Hexagonal prism	Hexagonal antiprism	Hexagonal pyramid

Tilings with regular hexagons			
Regular	1-uniform		
$\{6,3\}$ 	$r\{6,3\}$ 	$rr\{6,3\}$ 	$tr\{6,3\}$ 
			
2-uniform tilings			
			

## Gallery of natural and artificial hexagons



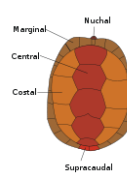
The ideal crystalline structure of graphene is a hexagonal grid.



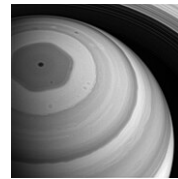
Assembled E-ELT mirror segments



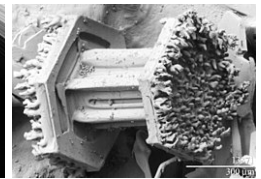
A beehive honeycomb



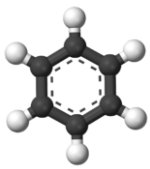
The scutes of a turtle's carapace



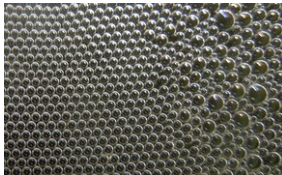
Saturn's hexagon, a hexagonal cloud pattern around the north pole of the planet



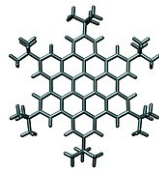
Micrograph of a snowflake



Benzene, the simplest aromatic compound with hexagonal shape.



Hexagonal order of bubbles in a foam.



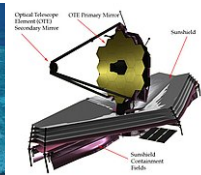
Crystal structure of a molecular hexagon composed of hexagonal aromatic rings.



Naturally formed basalt columns from Giant's Causeway in Northern Ireland; large masses must cool slowly to form a polygonal fracture pattern



An aerial view of Fort Jefferson in Dry Tortugas National Park



The James Webb Space Telescope mirror is composed of 18 hexagonal segments.





In French, *l'Hexagone* refers to Metropolitan France for its vaguely hexagonal shape.



Hexagonal Hanksite crystal, one of many hexagonal crystal system minerals



Hexagonal barn



The Hexagon, a hexagonal theatre in Reading, Berkshire



Władysław Guliński's hexagonal chess



Pavilion in the Taiwan Botanical Gardens



Hexagonal window

## See also

- 24-cell: a four-dimensional figure which, like the hexagon, has orthoplex facets, is self-dual and tessellates Euclidean space
- Hexagonal crystal system
- Hexagonal number
- Hexagonal tiling: a regular tiling of hexagons in a plane
- Hexagram: six-sided star within a regular hexagon
- Unicursal hexagram: single path, six-sided star, within a hexagon
- Honeycomb conjecture
- Havannah: abstract board game played on a six-sided hexagonal grid

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## External links

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- Definition and properties of a hexagon (<http://www.mathopenref.com/hexagon.html>) with interactive animation and construction with compass and straightedge (<http://www.mathopenref.com/consthexagon.html>).
- An Introduction to Hexagonal Geometry (<https://hexnet.org/content/hexagonal-geometry>) on Hexnet (<https://web.archive.org/web/19980204100717/http://www.hexnet.org/>) a website devoted to hexagon mathematics.
- Hexagons are the Bestagons (<https://www.youtube.com/watch?v=thOifuHs6eY>) on YouTube – an animated internet video about hexagons by CGP Grey.

Fundamental convex regular and uniform polytopes in dimensions 2–10					
Family	$A_n$	$B_n$	$I_2(p) / D_n$	$E_6 / E_7 / E_8 / E_4 / G_2$	$H_n$
<b>Regular polygon</b>	<a href="#">Triangle</a>	<a href="#">Square</a>	<a href="#">p-gon</a>	<a href="#">Hexagon</a>	<a href="#">Pentagon</a>
<b>Uniform polyhedron</b>	<a href="#">Tetrahedron</a>	<a href="#">Octahedron • Cube</a>	<a href="#">Demicube</a>		<a href="#">Dodecahedron • Icosahedron</a>
<b>Uniform polychoron</b>	<a href="#">Pentachoron</a>	<a href="#">16-cell • Tesseract</a>	<a href="#">Demitesseract</a>	<a href="#">24-cell</a>	<a href="#">120-cell • 600-cell</a>
<b>Uniform 5-polytope</b>	<a href="#">5-simplex</a>	<a href="#">5-orthoplex • 5-cube</a>	<a href="#">5-demicube</a>		
<b>Uniform 6-polytope</b>	<a href="#">6-simplex</a>	<a href="#">6-orthoplex • 6-cube</a>	<a href="#">6-demicube</a>	$1_{22} \cdot 2_{21}$	
<b>Uniform 7-polytope</b>	<a href="#">7-simplex</a>	<a href="#">7-orthoplex • 7-cube</a>	<a href="#">7-demicube</a>	$1_{32} \cdot 2_{31} \cdot 3_{21}$	
<b>Uniform 8-polytope</b>	<a href="#">8-simplex</a>	<a href="#">8-orthoplex • 8-cube</a>	<a href="#">8-demicube</a>	$1_{42} \cdot 2_{41} \cdot 4_{21}$	
<b>Uniform 9-polytope</b>	<a href="#">9-simplex</a>	<a href="#">9-orthoplex • 9-cube</a>	<a href="#">9-demicube</a>		
<b>Uniform 10-polytope</b>	<a href="#">10-simplex</a>	<a href="#">10-orthoplex • 10-cube</a>	<a href="#">10-demicube</a>		
<b>Uniform <math>n</math>-polytope</b>	<a href="#">n-simplex</a>	<a href="#">n-orthoplex • n-cube</a>	<a href="#">n-demicube</a>	$1_{k2} \cdot 2_{k1} \cdot k_{21}$	<a href="#">n-pentagonal polytope</a>
<b>Topics: <a href="#">Polytope families</a> • <a href="#">Regular polytope</a> • <a href="#">List of regular polytopes and compounds</a></b>					

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