

eg square root of $3+4i = ?$

$$\sqrt{3+4i} \rightarrow (1)$$

square root should be of $\sqrt{(a+ib)^2}$

$$= \sqrt{a^2-b^2+2abi} \rightarrow (2)$$

Comparing 1 and 2,

$$2ab = 4 \quad a^2 - b^2 = 3$$

$$\rightarrow ab = 2$$

\therefore 2 and 1 are the 2 nos with product = 2 & difference of squares as 3.

$$\Rightarrow \sqrt{3+4i} = \sqrt{2^2 - 1^2 + 2 \cdot 2 \cdot 1 \cdot i}$$

$$= \sqrt{2^2 + i^2 + 4i}$$

$$= \pm(2+i)$$

2) Find value of \sqrt{i}

$$\sqrt{i} \rightarrow \sqrt{a^2 - b^2 + 2abi}$$

$$\sqrt{i} = \sqrt{\frac{2i}{2}}$$

\therefore Finding for $\sqrt{2i}$

$$2ab = 2 \rightarrow ab = 1 \quad \& \quad a^2 - b^2 = 0$$

$$\Rightarrow a \text{ and } b = 1$$