

3. If given two circles are cutting each other then radical axis is their common chord.

Proof : Let the circles $s=0$, $s'=0$
intersect at $P(x_1, y_1)$ and $Q(x_2, y_2)$

As $P(x_1, y_1)$ lies on $s=0$ & $s'=0$

$$\Rightarrow s_{11} = 0 \quad \& \quad s'_{11} = 0$$

$$\Rightarrow s_{11} - s'_{11} = 0$$

It is very clear that $P(x_1, y_1)$ lies on $s - s' = 0$

Similarly $Q(x_2, y_2)$ lies on $s=0$ & $s'=0$

$$\Rightarrow s_{22} = 0 \quad \& \quad s'_{22} = 0$$

$$\Rightarrow s_{22} - s'_{22} = 0$$

It shows $Q(x_2, y_2)$ also lies on $s - s' = 0$

P & Q points both lie on $s - s' = 0$

$\therefore \overline{PQ}$ is a common chord which is the R.A.

